Mathematics Station Activities
for Common Core State Standards
Grade 7
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The standards correlations below support the implementation of the Common Core Standards. This book includes station activity sets for the Common Core domains of Ratios and Proportional Relationships; The Number System; Expressions and Equations; Geometry; and Statistics and Probability. The table below provides a listing of the available station activities organized by Common Core standard.

The left column lists the standard codes. The first number of the code represents the grade level. The grade number is followed by the initials of the Common Core domain name, which is then followed by the standard number. The middle column of the table lists the title of the station activity set that corresponds to the standard, and the right column lists the page number where the station activity set can be found.

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Introduction

This book includes a collection of station-based activities to provide students with opportunities to practice and apply the mathematical skills and concepts they are learning. It contains sets of activities for each of the five Grade 7 Common Core Mathematics strands: Ratios and Proportional Relationships; The Number System; Expressions and Equations; Geometry; and Statistics and Probability. You may use these activities in addition to direct instruction, or instead of direct instruction in areas where students understand the basic concepts but need practice. The Discussion Guide included with each set of activities provides an important opportunity to help students reflect on their experiences and synthesize their thinking. It also provides guidance for ongoing, informal assessment to inform instructional planning.

Implementation Guide

The following guidelines will help you prepare for and use the activity sets in this book.

Setting Up the Stations

Each activity set consists of four stations. Set up each station at a desk, or at several desks pushed together, with enough chairs for a small group of students. Place a card with the number of the station on the desk. Each station should also contain the materials specified in the teacher’s notes, and a stack of student activity sheets (one copy per student). Place the required materials (as listed) at each station.

When a group of students arrives at a station, each student should take one of the activity sheets to record the group’s work. Although students should work together to develop one set of answers for the entire group, each student should record the answers on his or her own activity sheet. This helps keep students engaged in the activity and gives each student a record of the activity for future reference.

Forming Groups of Students

All activity sets consist of four stations. You might divide the class into four groups by having students count off from 1 to 4. If you have a large class and want to have students working in small groups, you might set up two identical sets of stations, labeled A and B. In this way, the class can be divided into eight groups, with each group of students rotating through the “A” stations or “B” stations.
Assigning Roles to Students

Students often work most productively in groups when each student has an assigned role. You may want to assign roles to students when they are assigned to groups and change the roles occasionally. Some possible roles are as follows:

- **Reader**—reads the steps of the activity aloud
- **Facilitator**—makes sure that each student in the group has a chance to speak and pose questions; also makes sure that each student agrees on each answer before it is written down
- **Materials Manager**—handles the materials at the station and makes sure the materials are put back in place at the end of the activity
- **Timekeeper**—tracks the group’s progress to ensure that the activity is completed in the allotted time
- **Spokesperson**—speaks for the group during the debriefing session after the activities

Timing the Activities

The activities in this book are designed to take approximately 15 minutes per station. Therefore, you might plan on having groups change stations every 15 minutes, with a two-minute interval for moving from one station to the next. It is helpful to give students a “5-minute warning” before it is time to change stations.

Since the activity sets consist of four stations, the above time frame means that it will take about an hour and 10 minutes for groups to work through all stations. If this is followed by a 20-minute class discussion as described below, an entire activity set can be completed in about 90 minutes.

Guidelines for Students

Before starting the first activity set, you may want to review the following “ground rules” with students. You might also post the rules in the classroom.

- All students in a group should agree on each answer before it is written down. If there is a disagreement within the group, discuss it with one another.
- You can ask your teacher a question only if everyone in the group has the same question.
- If you finish early, work together to write problems of your own that are similar to the ones on the student activity sheet.
- Leave the station exactly as you found it. All materials should be in the same place and in the same condition as when you arrived.
Debriefing the Activities

After each group has rotated through every station, bring students together for a brief class discussion. At this time, you might have the groups’ spokespersons pose any questions they had about the activities. Before responding, ask if students in other groups encountered the same difficulty or if they have a response to the question. The class discussion is also a good time to reinforce the essential ideas of the activities. The questions that are provided in the teacher’s notes for each activity set can serve as a guide to initiating this type of discussion.

You may want to collect the student activity sheets before beginning the class discussion. However, it can be beneficial to collect the sheets afterward so that students can refer to them during the discussion. This also gives students a chance to revisit and refine their work based on the debriefing session.
Station Sets

- 2 bags (to hold cubes/blocks/etc.)
- 2 spinners (one divided evenly into red, green, blue, and yellow sections; the other divided evenly into black and white sections)
- 3 blocks (red, green, and blue)
- 3 marshmallows
- box of toothpicks
- clay
- colored cubes (one each of red, blue, and green; two yellow)
- graph paper
- integer chips
- list of 100 randomly generated numbers (1–9)
- marbles (24 green, 16 yellow)
- model car with scale factor
- optional: tape measure; water; separate containers to hold 1 cup, 1 quart, and 1 gallon of water
- plastic knives
- rectangular prism
- set of at least 5 congruent triangles
- tiles or small pieces of paper (several small square tiles; several small round tiles; 8 large blue algebra tiles; 20 small yellow algebra tiles)

Class Sets

- calculators
- compasses
- protractors
- rulers

Ongoing Use

- index cards (prepared according to specifications in teacher notes for many of the station activities)
- number cubes (several numbered 1–6; one numbered 4, 2, 2, 1, 3, 3; one numbered 6, 1, 3, 5, 4, 8)
- pencils
- pennies
- scrap/scratch paper
Ratios and Proportional Relationships

Set 1: Ratios and Proportions

Goal: To provide opportunities for students to develop concepts and skills related to unit conversion, finding percents, simplifying algebraic ratios, and solving algebraic proportions

Common Core Standards

Ratios and Proportional Relationships

Analyze proportional relationships and use them to solve real-world and mathematical problems.

7.RP.1. Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units.

7.RP.2. Recognize and represent proportional relationships between quantities.
   a. Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin.
   b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.
   c. Represent proportional relationships by equations.

7.RP.3. Use proportional relationships to solve multi-step ratio and percent problems. Examples: simple interest, tax, markups and markdowns, gratuities and commissions, fees, percent increase and decrease, percent error.

Student Activities Overview and Answer Key

Station 1

Students will be given 12 index cards with pairs of equivalent units of measurement written on them. They will work together to match the cards that are an equivalent unit of measurement. Then they will perform unit conversion.

Answers

1. 10 mm = 1 cm; 12 in. = 1 ft; 3 ft = 1 yd; 2 pints = 1 quart; 4 quarts = 1 gallon; 1 ton = 2,000 pounds
2. 8 pints in a gallon; 2 pints = 1 quart and 4 quarts = 1 gallon, so 2(4) = 8 pints
3. 18 inches; 1/2 yard = 1.5 feet and 12 inches = 1 foot, so 12(1.5) = 18 inches
4. 5,000 pounds
5. 850 mm
6. 13.5 feet
7. 3 quarts = 0.75 gallons
8. Answers will vary. Possible answers include: cooking, when modifying recipes for more or fewer people; carpentry, when creating custom-size cabinetry

Station 2
Students will be given a calculator to help them solve the problems. They work as a group to solve real-world applications of unit conversions.

Answers
1. His friend measures temperature in Celsius, and Evan measures it in Fahrenheit. $F = 95^\circ$
2. $P = 36.67$ yards; $P = 1,320$ inches, $A = 77.78$ yds$^2$; $A = 100,800$ in$^2$
3. 

<table>
<thead>
<tr>
<th></th>
<th>Feet</th>
<th>Yards</th>
<th>Meters</th>
<th>Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tim</td>
<td>300</td>
<td>100</td>
<td>91.44</td>
<td>12 seconds</td>
</tr>
<tr>
<td>Jeremy</td>
<td>400</td>
<td>133.33</td>
<td>121.95</td>
<td>12 seconds</td>
</tr>
<tr>
<td>Martin</td>
<td>229.66</td>
<td>76.55</td>
<td>70</td>
<td>12 seconds</td>
</tr>
</tbody>
</table>

Jeremy, Tim, Martin; Tim = 25 feet/sec, Jeremy = 33.33 feet/sec; Martin = 19.14 feet/sec

Station 3
Students will be given a bag containing 24 green marbles and 16 yellow marbles. They will use the marbles to create ratios and percents. They will then solve percent problems.

Answers
1. Answers will vary. Possible answers include: green = 1; yellow = 7; total = 8. Find $1/8 = 0.125 = 12.5$%; 12.5% were green. Subtract 12.5% from 100% to get 87.5% or 7/8 = 87.5%; 87.5% were yellow.
2. There are 40 marbles so $24/40 = 60\%$ green marbles; $100\% - 60\% = 40\%$ or $16/40 = 40\%$
3. 9 yellow marbles; student drawings should depict 9 yellow marbles and 12 green marbles.
4. $24(1/4) = 6$ or $24(0.25) = 6$
5. $17(2/1) = 34$ or $17(2.0) = 34$
6. $10(14) = 140$ in$^2$; increased dimensions by 200% then found the area of the photograph
Ratios and Proportional Relationships
Set 1: Ratios and Proportions

Station 4

Students will be given 8 large blue algebra tiles and 20 small yellow algebra tiles. Students visually depict ratios and proportions with the algebra tiles. They then solve proportions for a specified variable including a real-world application.

Answers

1. \[ \frac{8 \text{ blue}}{20 \text{ yellow}} = \frac{2}{5} \]
2. \[ \frac{2 \text{ blue}}{3 \text{ yellow}} = \frac{4 \text{ blue}}{6 \text{ yellow}} \]
3. \[ \frac{8}{20} = \frac{x}{100}, \text{ so } x = 40 \text{ blue} \]
4. \[ \frac{8}{20} = \frac{x}{15}, \text{ so } x = 6 \text{ blue} \]
5. \[ x = 4 \]
6. \[ x = 40 \]
7. \[ \frac{\text{blue}}{\text{yellow}} = \frac{6}{10} = \frac{3}{5} \]

Let \( x \) = number of blue pencils and 24 – \( x \) = number of yellow pencils.

\[ \frac{3}{5} = \frac{x}{(24 - x)}, \text{ so } x = 9 \text{ blue pencils and } 24 - x = 15 \text{ yellow pencils} \]

Materials List/Setup

Station 1 12 index cards with the following written on them:
10 millimeters, 12 inches, 3 feet, 2 pints, 4 quarts, 1 ton, 1 centimeter, 1 foot, 1 yard, 1 quart, 1 gallon, 2,000 pounds

Station 2 calculator

Station 3 24 green marbles; 16 yellow marbles

Station 4 8 large blue algebra tiles; 20 small yellow algebra tiles
Ratios and Proportional Relationships
Set 1: Ratios and Proportions

Discussion Guide
To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions
1. How do you perform unit conversion?
2. When would you use unit conversion in the real world?
3. What are two ways to find the percent of a number?
4. What is a ratio?
5. How do you know if two ratios are equivalent?
6. What is a proportion?
7. When would you use ratios and proportions in the real world?

Think, Pair, Share
Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses
1. Use ratios and proportions to convert units.
2. Answers will vary. Possible answers include: creating scale models of buildings; using the metric system instead of U.S. Customary units; converting Celsius to degrees Fahrenheit and vice versa
3. Multiply the number by a decimal or fraction that represents the percentage.
4. A ratio is a comparison of two numbers by division.
5. Two ratios are equivalent if, when simplified, they are equal.
6. A proportion is when two ratios are set equal to each other.
7. Answers will vary. Possible answers include: enlarging photos; scale models; modifying quantities of ingredients in a recipe
Ratios and Proportional Relationships
Set 1: Ratios and Proportions

Possible Misunderstandings/Mistakes

- Not keeping track of units and using incorrect unit conversions
- Not recognizing that terms must have the same units in order to compare them
- Setting up proportions with one of the ratios written with the incorrect numbers in the numerator and denominator
- Not recognizing simplified forms of ratios in order to find equivalent ratios
Station 1
You will be given 12 index cards with the following written on them:
10 millimeters, 12 inches, 3 feet, 2 pints, 4 quarts, 1 ton, 1 centimeter, 1 foot, 1 yard,
1 quart, 1 gallon, 2,000 pounds

Shuffle the index cards and deal a card to each student in your group until all the cards are gone. As a group, show your cards to each other and match the cards that are an equivalent unit of measurement.

1. Write your answers on the lines below. The first match is shown:

   10 mm = 1 cm

2. Find the number of pints in a gallon. Explain how you can use your answers in problem 1 to find the number of pints in a gallon.

3. Find the number of inches in half of a yard. Explain how you can use your answers in problem 1 to find the number of inches in half of a yard.
Perform the following unit conversions by filling in the blanks.

4. 2.5 tons = _____ pounds

5. 85 cm = _____ mm

6. 4.5 yd = _____ ft

7. 6 pints = _____ quarts = _____ gallons

8. When would you use unit conversions in the real world?
Station 2
You will be given a calculator to help you solve the problems. Work as a group to solve these real-world applications of unit conversions.

1. Evan has a friend in England. His friend said the temperature was very hot at 35°. Evan thought he heard his friend incorrectly since 35° is cold. What caused his misunderstanding?

   (Hint: \( C = (F - 32) \frac{5}{9} \))

Find the equivalent temperature in the United States that would make the claim of Evan’s friend valid. Write your answer in the space below.

2. Anna is going to build a patio. She wants the patio to be 20 feet by 35 feet. What is the perimeter of the patio in yards?

   What is the perimeter of the patio in inches?

   What is the area of the patio in yards?
What is the area of the patio in inches?

3. Tim claims he can run the 100-yard dash in 12 seconds. Jeremy claims he can run 400 feet in 12 seconds. Martin claims he can run 70 meters in 12 seconds. *(Hint: 1 yard = 0.9144 meters and 1 yard = 3 feet.)*

Fill in the table below to create equivalent units of measure.

<table>
<thead>
<tr>
<th></th>
<th>Feet</th>
<th>Yards</th>
<th>Meters</th>
<th>Time (seconds)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tim</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Jeremy</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Martin</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

List the three boys in order of fastest to slowest:

How fast did each boy run in feet/second?
Station 3
You will be given a bag containing 24 green marbles and 16 yellow marbles. You will use the marbles to create ratios and percents. You will then solve percent problems. Work together as a group to solve the following problems.

1. Shake the bag of green and yellow marbles so that the colors are mixed. Have each student select 2 marbles from the bag without looking. Group all your marbles together by color.
   
   How many green marbles did you draw? _____________
   How many yellow marbles did you draw? _____________
   What was the total number of marbles drawn? ___________
   How can you determine the percentage of marbles that were green?

   Find the percentage of marbles you drew that were green.

   Name two ways you can find the percentage of marbles you drew that were yellow.

   Find the percentage of marbles you drew that were yellow.

2. Take all the marbles out of the bag. How can you determine what percentage of all the marbles are green?

   How can you determine what percentage of all the marbles are yellow?
3. Place 12 green marbles on the table. How many yellow marbles do you need to have 75% as many yellow marbles on the table?

Draw a picture of the number of green marbles and yellow marbles you have placed on the table.

4. Use equations to show two ways you can find 25% of 24.

5. Use equations to show two ways you can find 200% of 17.

6. Real-world application: Bryan is a photographer. He has a 5 in. by 7 in. photo that he wants to enlarge by 200%. What is the area of the new photo? Explain your answer in the space below.
Station 4

You will be given 8 large blue algebra tiles and 20 small yellow algebra tiles. Work as a group to arrange the algebra tiles so they visually depict the ratio of blue to yellow algebra tiles.

1. What is this ratio? ________________

Rearrange the tiles to visually depict the following ratios:

<table>
<thead>
<tr>
<th>2 blue</th>
<th>1 blue</th>
<th>4 blue</th>
<th>1 blue</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 yellow</td>
<td>10 yellow</td>
<td>6 yellow</td>
<td>1 yellow</td>
</tr>
</tbody>
</table>

2. Which ratios are equivalent ratios? Explain your answer.

3. Keeping the same ratio of yellow to blue tiles, if there were 100 yellow algebra tiles, how many blue algebra tiles would there be? Use a proportion to solve this problem. Show your work in the space below. (Hint: A proportion is two ratios that are equal to each other.)

4. Keeping the same ratio of yellow to blue tiles, if there were 15 yellow algebra tiles, how many blue algebra tiles would there be? Use a proportion to solve this problem. Show your work in the space below.
Work together to solve the following proportions for the variable.

5. \( \frac{2}{7} = \frac{x}{14} ; x = \)

6. \( \frac{8}{x} = \frac{2}{10} ; x = \)

Use the following information to answer problem 7:

Allison has 6 blue pencils and 10 yellow pencils. Sadie has 24 pencils that are either blue or yellow. The ratio of blue pencils to yellow pencils is the same for both Allison and Sadie.

7. How many blue pencils and yellow pencils does Sadie have? Show your work in the space below by setting up a proportion using a variable, \( x \).
Ratios and Proportional Relationships

Set 2: Problem Solving with Rational Numbers

Instruction

Goal: To provide opportunities for students to solve problems involving rational numbers

Common Core Standards

Ratios and Proportional Relationships
Analyze proportional relationships and use them to solve real-world and mathematical problems.

7.RP.3. Use proportional relationships to solve multistep ratio and percent problems. Examples: simple interest, tax, markups and markdowns, gratuities and commissions, fees, percent increase and decrease, percent error.

Expressions and Equations
Solve real-life and mathematical problems using numerical and algebraic expressions and equations.

7.EE.3. Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.

Student Activities Overview and Answer Key

Station 1
Students work together to solve a real-world problem involving percent discounts. Students are encouraged to brainstorm appropriate problem-solving strategies and to explain their solution process once all students in the group agree upon the solution.

Answers: The regular price was $60.
Possible strategies: Work backward.
Possible steps: Work backward to find that the price before Wednesday’s discount was $36, before Tuesday’s discount was $45, and before Monday’s discount was $60.

Station 2
Students work together to solve a real-world problem involving coins. This requires students to do arithmetic with rational numbers in the form of decimals. After reading the problem, students brainstorm possible problem-solving strategies. Students are encouraged to make sure everyone in the group agrees on the solution. Then students explain their solution process.
Answers: 15 quarters and 6 nickels

Possible strategies: Guess and check various possibilities; make an organized list of all possible combinations of quarters and nickels.

Possible steps: Try various combinations of quarters and nickels that add up to a total of 21 coins. Find the total value of the coins. Adjust the guesses to find a combination for which the total value of the coins is $4.05.

Station 3

Students work together to solve a real-world problem involving fractions. Students are encouraged to brainstorm different strategies that may be used to solve the problem and to make sure everyone in the group agrees on the solution. (The problem is especially well-suited to drawing a diagram.) Students write an explanation of their solution process.

Answers: 24 posts

Possible strategies: Draw a diagram.

Possible steps: Draw a rectangle and mark the dimensions of the plot. Mark the posts around the edge of the plot, noting that every four posts will span 9 feet of the perimeter. Count the total number of posts needed.

Station 4

Students work together to solve a real-world problem involving the ratio of girls to boys at a school. Students can solve the problem in many ways, including using proportional reasoning. After reading the problem, students brainstorm possible problem-solving strategies. Students are encouraged to make sure everyone in the group agrees on the solution. Then students explain their solution process.

Answers: 51 girls and 34 boys

Possible strategies: Guess and check various possibilities; find different combinations of girls and boys in which the number of girls is $1\frac{1}{2}$ times the number of boys, and increase or decrease the numbers of girls and boys proportionally until the total number of students is 85.

Possible steps: Try various combinations of girls and boys, such as 30 girls and 20 boys, in which the number of girls is $1\frac{1}{2}$ times the number of boys. Continue until the total number of students is exactly 85. Alternatively, find combinations of numbers that have a sum of 85 and adjust the numbers until they differ by a factor of $1\frac{1}{2}$.

Materials List/Setup

No materials needed
Ratios and Proportional Relationships
Set 2: Problem Solving with Rational Numbers

Discussion Guide

To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions

1. What are some different problem-solving strategies you can use to help you solve real-world problems?
2. How do you perform arithmetic operations involving percents when you solve a problem?
3. How do you decide when to use a diagram to help you solve a problem?
4. How can you check your answer to a real-world problem?

Think, Pair, Share

Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses

1. Make a table, guess and check, look for a pattern, work backward, draw a diagram, use physical objects to model the problem, etc.
2. First convert the percents to decimals.
3. Use a diagram when the problem involves geometric shapes or relationships, or when the information can be represented on a number line.
4. Reread the problem using the answer in place of the unknown quantity or quantities. Check to see if the numbers work out correctly throughout the problem.

Possible Misunderstandings/Mistakes

- Incorrectly converting percents to decimals
- Using the amount of a discount as the sale price (e.g., writing $25 as the sale price of a $100 item that is discounted by 25%)
- Incorrectly using decimals to write the value of coins (e.g., writing 5 or 0.5 for the value of a nickel instead of 0.05)
Ratios and Proportional Relationships
Set 2: Problem Solving with Rational Numbers

Station 1
At this station, you will work with other students to solve this real-life problem.

A department store is having a special sale. On Monday, the regular price of a dress is marked down by 25%. On Tuesday, the dress is marked down by 20% of its current price. On Wednesday, the dress is marked down by 25% of its current price. After all the discounts, the final price of the dress is $27. What was the regular price of the dress?

Work with other students to discuss the problem. Brainstorm strategies you might use to solve the problem. Write the strategies below.

__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________

Solve the problem. When everyone agrees on the answer, write it below.

_____________________________________

Explain the steps you used to solve the problem.

__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
Station 2

At this station, you will work with other students to solve this real-life problem.

Latrell has a jar containing quarters and nickels. There are 21 coins in the jar altogether. The total value of the coins is $4.05. How many quarters and how many nickels are in the jar?

Work with other students to discuss the problem. Brainstorm strategies you might use to solve the problem. Write the strategies below.

__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________

Solve the problem. When everyone agrees on the answer, write it below.

___________________

Explain the steps you used to solve the problem.

__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
Station 3
At this station, you will work with other students to solve this real-life problem.

Anna wants to put a fence around a rectangular garden plot that measures 9 feet by 18 feet. She wants to place posts at the corners of the plot and every $2 \frac{1}{4}$ feet around the perimeter of the plot. How many posts does she need?

Work with other students to discuss the problem. Brainstorm strategies you might use to solve the problem. Write the strategies below.

__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________

Solve the problem. When everyone agrees on the answer, write it below.

___________________

Explain the steps you used to solve the problem.

__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
At Harriet Tubman Middle School, there are 85 students in the 7th grade. The number of girls is $\frac{1}{2}$ times the number of boys. How many girls and how many boys are in the 7th grade?

Work with other students to discuss the problem. Brainstorm strategies you might use to solve the problem. Write the strategies below.

__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________

Solve the problem. When everyone agrees on the answer, write it below.

___________________

Explain the steps you used to solve the problem.

__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
Ratios and Proportional Relationships
Set 3: Analyzing and Describing Relationships

Goal: To provide opportunities for students to develop concepts and skills related to analyzing and describing relationships

Common Core Standards

Ratios and Proportional Relationships
Analyze proportional relationships and use them to solve real-world and mathematical problems.

  7.RP.2. Recognize and represent proportional relationships between quantities.
      b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.
      c. Represent proportional relationships by equations.

Student Activities Overview and Answer Key

Station 1
In this activity, students work together to translate verbal phrases into algebraic expressions. Students are given information about a library’s late fees. They translate this information into algebraic expressions that can be used to calculate the late fees. Students explain their work and use their expressions to calculate late fees.

Answers
1. $0.75, $1, $1.75
2. $0.5 + 0.25d
3. The fee is $0.25 per day (which can be written as 0.25d) plus $0.50, so the total fee is 0.5 + 0.25d.
4. 2 + 0.5d
5. 1.5d
6. Evaluate 1.5d for d = 8, so the fee is 1.5(8) = $12.

Station 2
Students work together to analyze a pattern based on the cost of renting DVDs. They work together to complete and extend a table of values. Then students write an expression that can be used to find the cost of renting any number of DVDs. Finally, they use the expression to find the cost of renting 15 DVDs.
Ratios and Proportional Relationships
Set 3: Analyzing and Describing Relationships

Answers

The missing table values are $17, $20, and $23.
1. $26, $29
2. Possible explanation: Extend the table by adding $3 for each additional DVD.
3. $8 + 3m$
4. Possible explanation: The cost of renting $m$ DVDs is $8 plus $3 per DVD, which is $8 + 3m$.
5. The cost of renting 15 DVDs is $8 + 3(15) = $53.

Station 3

Students work together to analyze and extend a pattern that is provided in the form of a table. The table shows the (decreasing) number of contestants on a TV show from one week to the next. Students are asked to write and use an expression that describes the number of contestants during any given week.

Answers

1. 30 contestants
2. Extend the table to the 8th week by subtracting 6 contestants each week.
3. $72 − 6(x − 1)$ or $78 − 6x$
4. In week $x$, a total of 6 times $x−1$ contestants have been eliminated, so subtract $6(x−1)$ from 72.
5. In week 10, the number of contestants is $72 − 6(9) = 72 − 54 = 18$.

Station 4

At this station, students analyze and describe a relationship that is given in a graph. The graph shows the cost of renting ice skates for various numbers of hours. Students work together to predict the cost for a number of hours that is not shown on the graph. They also write and use an expression that gives the cost for $h$ hours.

Answers

1. $3, $5, $7$
2. $13$
3. The cost is 2 times the number of hours plus $1$. (Students may also extend the graph.)
4. $2h + 1$
5. To find the cost for 8 hours, let $h = 8$ in the expression to get $2(8) + 1 = $17$.

Materials List/Setup

No materials needed
Ratios and Proportional Relationships  
Set 3: Analyzing and Describing Relationships

Discussion Guide
To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions
1. What are some strategies you can use to help translate verbal phrases into algebraic expressions?
2. What are some strategies you can use to help extend a table of data?
3. Why is it useful to translate information from tables or graphs into algebraic expressions?
4. How can you use an expression that gives the cost of \(n\) apples to find the cost of 7 apples?

Think, Pair, Share
Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses
1. Use verbal clues about operations. For example, the word plus means “addition,” which will be represented by a “+” symbol in the algebraic expression.
2. Look for a pattern in the sequence of numbers. For example, a fixed number may be added or subtracted each time you go from one number to the next.
3. The algebraic expression is more general. You can use it to calculate additional values that are not shown in the table or graph.
4. Evaluate the expression for \(n = 7\).

Possible Misunderstandings/Mistakes
• Assuming that all patterns may be described multiplicatively (e.g., in the form \(y = kx\))
• Incorrectly representing operations when writing an expression (e.g., writing \(n + 2\) instead of \(2n\))
• Multiplying the variable by an incorrect constant (e.g., writing \(8m + 3\) instead of \(8 + 3m\))
Station 1

At this station, you will work with other students to translate words into algebra. Use the following information.

<table>
<thead>
<tr>
<th>Midtown Library</th>
</tr>
</thead>
<tbody>
<tr>
<td>Late Fees</td>
</tr>
<tr>
<td>Books: $0.50, plus $0.25 for each day that the book is late</td>
</tr>
<tr>
<td>CDs: $2, plus $0.50 for each day that the CD is late</td>
</tr>
<tr>
<td>DVDs: $1.50 per day that the DVD is late</td>
</tr>
</tbody>
</table>

Work together to complete the following. When everyone agrees on an answer, write it in the space provided.

1. What is the fee for a book that is 1 day late? 2 days late? 5 days late? ____________________

2. Write an expression that gives the fee for a book that is $d$ days late. _____________________

3. Explain how you came up with your answer to problem 2. ___________________________
   ______________________________________________________________________________
   ______________________________________________________________________________
   ______________________________________________________________________________

4. Write an expression that gives the fee for a CD that is $d$ days late. ______________________

5. Write an expression that gives the fee for a DVD that is $d$ days late. _____________________

6. Show how to use an expression you wrote to find the fee for a DVD that is 8 days late.
Station 2

At this station, you will explore a pattern based on prices.

Renting DVDs costs $8 for a membership, plus $3 for each DVD rented. The table shows the cost of renting different numbers of DVDs.

Work with other students to complete the table.

<table>
<thead>
<tr>
<th>Number of DVDs</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cost</td>
<td>$11</td>
<td>$14</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Work together to complete the following. When everyone agrees on an answer, write it in the space provided.

1. Predict the cost of renting 6 DVDs and 7 DVDs. ____________________

2. Explain how you made these predictions. ______________________________________
   _______________________________________________________________________
   _______________________________________________________________________
   _______________________________________________________________________

3. Write an expression that gives the cost of renting \( m \) DVDs. _______________]

4. Explain how you came up with the expression. _______________________________
   _______________________________________________________________________
   _______________________________________________________________________
   _______________________________________________________________________

5. Show how you can use your expression to find the cost of renting 15 DVDs.
Station 3

At this station, you will explore a pattern based on a table of data.

A television show begins with 72 contestants during the first week. Each week, 6 contestants are eliminated from the show. The table below shows the number of contestants during the first few weeks of the show.

<table>
<thead>
<tr>
<th>Week</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of contestants</td>
<td>72</td>
<td>66</td>
<td>60</td>
<td>54</td>
</tr>
</tbody>
</table>

Work together to complete the following. When everyone agrees on an answer, write it in the space provided.

1. Predict the number of contestants on the show during the 8th week. ____________________

2. Explain how you made this prediction. _________________________________________
   _______________________________________________________________________
   _______________________________________________________________________
   _______________________________________________________________________

3. Write an expression that gives the number of contestants during week $x$ of the show.
   ____________________

4. Explain how you came up with the expression. ____________________
   _______________________________________________________________________
   _______________________________________________________________________
   _______________________________________________________________________

5. Show how you can use the expression to find the number of contestants during the 10th week of the show.
Station 4

At this station, you will work with other students to analyze data in a graph.

The graph to the right shows the cost of renting ice skates for various numbers of hours.

Work together to solve the following problems. When everyone agrees on an answer, write it in the space provided.

1. What does it cost to rent ice skates for 1 hour? 2 hours? 3 hours?

______________________________________________________________________

2. Predict the cost of renting skates for 6 hours. ____________________

3. Explain how you made this prediction. ______________________________________
______________________________________________________________________
______________________________________________________________________
______________________________________________________________________

4. Write an expression that gives the cost of renting skates for \( h \) hours. ____________________

5. Show how you can use your expression to find the cost of renting skates for 8 hours.
Goal: To provide opportunities for students to develop concepts and skills related to coordinate graphing

Common Core Standards

Ratios and Proportional Relationships

Analyze proportional relationships and use them to solve real-world and mathematical problems.

7.RP.2. Recognize and represent proportional relationships between quantities.
   a. Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin.
   b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.
   c. Represent proportional relationships by equations.

Student Activities Overview and Answer Key

Station 1

Students work together to complete a table for the function \( y = x + 4 \). They use the completed table to write ordered pairs that satisfy the function, and then they work together to plot these points on a coordinate plane. Once students have plotted the points, they draw and describe the complete graph.

Answers

1. | \( x \) | \( y \) |
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>−5</td>
<td>−1</td>
</tr>
<tr>
<td>−1</td>
<td>3</td>
</tr>
<tr>
<td>0</td>
<td>4</td>
</tr>
<tr>
<td>2</td>
<td>6</td>
</tr>
<tr>
<td>3</td>
<td>7</td>
</tr>
</tbody>
</table>

2. (−5, −1), (−1, 3), (0, 4), (2, 6), (3, 7)
Ratios and Proportional Relationships
Set 4: Graphing Relationships

3–5.

6. The graph is an upward-sloping straight line.

Station 2

In this activity, students are given a table of values. They work together to plot these points and look for patterns. (The points all satisfy the relationship \( y = -2x + 3 \), so they all lie on a straight line.) Using the graph of plotted points, students name an additional point that they think satisfies the same relationship, and they justify their choice.

Answers
1. \((-5, 13), (-2, 7), (0, 3), (3, -3), (4, -5)\)
2–3.
4. The points all lie on a straight line.
5. Possible answer: (–3, 9) or (2, –1).
6. The point lies along the line determined by the other points.

Station 3

Students work together to explore a pattern made from tiles. They complete a table showing the relationship between the stage of the pattern and the number of tiles needed. Then they plot the points (which lie on the line $y = 3x + 1$) and use the graph to predict the number of tiles that would be needed to make Stage 8 of the pattern.

Answers

1. 

<table>
<thead>
<tr>
<th>Stage (x)</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of tiles (y)</td>
<td>4</td>
<td>7</td>
<td>10</td>
<td>13</td>
<td>16</td>
</tr>
</tbody>
</table>

2. (1, 4), (2, 7), (3, 10), (4, 13), (5, 16)

3–4. ![Graph](image)

5. 25 tiles

6. Possible explanation: The plotted points all lie on a line. Continue the pattern of points until the $x$-value is 8. The point is (8, 25).
Station 4

Students work together to explore and graph a relationship based on a real-life situation. First, students complete a table of values that show the temperature of a freezer at various times. Then they work together to plot the points. They use their graph to predict the number of hours it will take for the temperature of the freezer to be 2°F.

Answers

1. 

<table>
<thead>
<tr>
<th>Hour (x)</th>
<th>0</th>
<th>1</th>
<th>4</th>
<th>7</th>
<th>9</th>
</tr>
</thead>
<tbody>
<tr>
<td>Temperature, °F (y)</td>
<td>20</td>
<td>17</td>
<td>8</td>
<td>-1</td>
<td>-7</td>
</tr>
</tbody>
</table>

2. (0, 20), (1, 17), (4, 8), (7, -1), (9, -7)

3–4. 

5. 6 hours

6. The plotted points all line on a straight line. Find the point along this line where the y-value is 2 (this corresponds to 2°F). The point is (6, 2).

Materials List/Setup

Station 1  graph paper; ruler
Station 2  graph paper; ruler
Station 3  small square tiles; graph paper; ruler
Station 4  graph paper; ruler
Discussion Guide

To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions
1. How do you set up a coordinate plane on a sheet of graph paper?
2. How do you plot an ordered pair on a coordinate plane?
3. How do you get ordered pairs from a table of values?
4. Is the ordered pair (2, 5) the same as the ordered pair (5, 2)? Why or why not?

Think, Pair, Share

Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses
1. Use a ruler to draw a straight line (x-axis). Draw another line at a right angle to the first line (y-axis). Label the intersection as the origin, (0, 0).
2. First plot the x-value by moving along the x-axis by the given number of units (right if the x-value is positive, left if it is negative). Then move up or down from this point to plot the y-value (up if the y-value is positive, down if it is negative).
3. In each row or column, take the x-value and the corresponding y-value, in that order, to form one ordered pair.
4. No. In (2, 5), the x-value is 2 and the y-value is 5. In (5, 2), the x-value is 5 and the y-value is 2. These are different points on the coordinate plane.

Possible Misunderstandings/Mistakes
- Plotting points incorrectly due to reversing the x- and y-values (e.g., plotting (3, 4) rather than (4, 3))
- Plotting points incorrectly due to mislabeling or incorrectly calibrating the scale on the x- or y-axis
- Incorrectly reading the ordered pairs from a table of values
Station 1

At this station, you will work together to make a table and graph for the equation $y = x + 4$.

The equation $y = x + 4$ states that the value of $y$ is equal to the value of $x$ plus 4.

1. Work with other students to complete the table of values.

<table>
<thead>
<tr>
<th>$x$</th>
<th>$y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>−5</td>
<td></td>
</tr>
<tr>
<td>−1</td>
<td></td>
</tr>
<tr>
<td>0</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td></td>
</tr>
</tbody>
</table>

2. Write the ordered pairs of values, $(x, y)$, from your table.

3. Set up a coordinate plane on a sheet of graph paper. Use a ruler to draw the $x$-axis and the $y$-axis.

4. Plot the ordered pairs from your table. Work together to make sure that all the points are plotted correctly.

5. Use the points to draw the complete graph of the equation $y = x + 4$.

6. Describe the graph of the equation $y = x + 4$. 

__________________________________________________________________
__________________________________________________________________
__________________________________________________________________
__________________________________________________________________
__________________________________________________________________
__________________________________________________________________
Station 2

At this station, you will plot points from a table and use your graph to make predictions.

The table shows a set of values. Work with other students to explore how the x- and y-values are related.

<table>
<thead>
<tr>
<th>x</th>
<th>y</th>
</tr>
</thead>
<tbody>
<tr>
<td>-5</td>
<td>13</td>
</tr>
<tr>
<td>-1</td>
<td>7</td>
</tr>
<tr>
<td>0</td>
<td>3</td>
</tr>
<tr>
<td>3</td>
<td>-3</td>
</tr>
<tr>
<td>4</td>
<td>-5</td>
</tr>
</tbody>
</table>

1. Write the ordered pairs of values, \((x, y)\), from the table.

2. Set up a coordinate plane on a sheet of graph paper. Use a ruler to draw the \(x\)-axis and the \(y\)-axis.

3. Plot the ordered pairs. Work together to make sure that all the points are plotted correctly.

4. Describe what you notice about the points.

5. Add a new point to the graph that you think has the same relationship between the \(x\)-value and \(y\)-value. What are the coordinates of the point?

6. Explain how you decided on this point.
Station 3

At this station, you will use a table and graph to explore a pattern. You can also use tiles to build the pattern.

Andre is using tiles to make a pattern for a walkway in his garden. Here are the first three stages in his pattern.

<table>
<thead>
<tr>
<th>Stage (x)</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of tiles (y)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

1. Complete the table.

2. Write the ordered pairs of values, \((x, y)\), from the table.

3. Set up a coordinate plane on a sheet of graph paper. Use a ruler to draw the \(x\)-axis and the \(y\)-axis.

4. Plot the ordered pairs. Work together to make sure that all the points are plotted correctly.

5. Use your graph to predict the number of tiles that are needed at Stage 8.

6. Explain how you made this prediction.
Station 4

Work together to analyze a table of data from a real-life situation.

A scientist is doing an experiment with bacteria in a freezer. She sets the temperature of the freezer to 20°F. Each hour, she decreases the temperature by 3°F.

1. Complete the table.

<table>
<thead>
<tr>
<th>Hour (x)</th>
<th>0</th>
<th>1</th>
<th>4</th>
<th>7</th>
<th>9</th>
</tr>
</thead>
<tbody>
<tr>
<td>Temperature, °F (y)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

2. Write the ordered pairs of values, \((x, y)\), from the table.

______________________________________________________________________

3. Set up a coordinate plane on a sheet of graph paper. Use a ruler to draw the \(x\)-axis and the \(y\)-axis.

4. Plot the ordered pairs. Work together to make sure that all the points are plotted correctly.

5. Use your graph to predict the number of hours it will take for the temperature in the freezer to reach 2°F.

_______ hours

6. Explain how you made this prediction.

______________________________________________________________________

______________________________________________________________________

______________________________________________________________________
Instruction

Goal: To provide opportunities for students to develop concepts and skills related to representing patterns and relationships

Common Core Standards

Ratios and Proportional Relationships

7.RP.2. Recognize and represent proportional relationships between quantities.

b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.

c. Represent proportional relationships by equations.

Student Activities Overview and Answer Key

Station 1

Students build, extend, and describe a geometric pattern made of toothpicks. Students are asked to work together to predict the number of toothpicks that would be needed to build the 10th stage of the pattern, and they are asked to write an expression that gives a general rule for the pattern.

Answers

1. 17, 21

2. 41

3. Possible answer: Multiply the number of the stage by 4 and add 1.

4. 4x + 1

5. Possible explanation: To find the number of toothpicks, multiply the number of the stage by 4 and then add 1. So if the number of the stage is x, then the number of toothpicks is 4x + 1.

Station 2

Students work together to analyze a pattern based on the cost of renting a car. They work together to complete a table of values. Then students write an expression that can be used to find the cost of renting a car for any number of days. They use the expression to find the cost of renting a car for 14 days and work backward (or write an equation) to find the number of days for which a car was rented if the total cost was $335.
Ratios and Proportional Relationships
Set 5: Representing Patterns and Relationships

Answers

Missing table values: 7 days, $195, $300

1. \(20 + 35d\)

2. The cost \(c\) is $20 plus $35 per day, or \(20 + 35d\).

3. The cost is \(20 + 35(14) = 510\)

4. 9 days

5. Find a value of \(d\) so that \(20 + 35d = 335\). Use guess and check, or solve the equation algebraically.

Station 3

Students work together to make their own table based on a given situation about the number of buses needed to transport various numbers of students. Students write an expression for the pattern in the table and then use the expression to answer questions and make predictions about the real-world situation.

Answers

Sample table:

<table>
<thead>
<tr>
<th>Number of buses ((b))</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of students ((s))</td>
<td>24</td>
<td>48</td>
<td>72</td>
<td>96</td>
<td>120</td>
</tr>
</tbody>
</table>

1. \(24b\)

2. There are 24 students per bus, so the number of students for \(b\) buses is \(24b\).

3. The number of students is \(24(12) = 288\).

4. 9 buses. Find a value of \(b\) for which \(24b = 216\) and find that \(b = 9\).

Station 4

Students build, describe, and make predictions about a geometric pattern. To do so, they may use physical objects to model the pattern. Students work together to write expressions that describe various aspects of the geometric pattern.
Answers
1. 8 circular stickers and 25 square stickers
2. The number of circular stickers is equal to the number of the stage. The number of square stickers is 3 times number of the stage plus 1.
3. \( n \)
4. \( 3n + 1 \)
5. \( 4n + 1 \)

Materials List/Setup
- Station 1: box of toothpicks
- Station 2: none
- Station 3: none
- Station 4: small square tiles and small round tiles
Ratios and Proportional Relationships
Set 5: Representing Patterns and Relationships

Discussion Guide

To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions

1. What are some different tools, objects, or drawings that you can use to help you analyze a pattern?
2. What strategies can you use to help you translate information from words or tables into an algebraic expression?
3. Why is it useful to express relationships as algebraic expressions?
4. Is it ever possible for there to be more than one correct way to write an expression that represents a situation? Explain.

Think, Pair, Share

Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses

1. hands-on manipulatives, drawings of patterns, tables, etc.
2. Use verbal clues about operations. For example, the word “plus” means addition, which will be represented by a “+” symbol in the algebraic expression.
3. Algebraic expressions are more general than tables or graphs. You can use an expression to calculate additional values that are not shown in the table or graph.
4. Yes. For example, the expression $4s + 1$ can also be written as $1 + 4s$.

Possible Misunderstandings/Mistakes

- Incorrectly representing operations when writing an expression (e.g., writing $n + 2$ instead of $2n$)
- Multiplying the variable by an incorrect constant (e.g., writing $35 + 20d$ instead of $20 + 35d$)
- Incorrectly evaluating an expression for a specific value of the variable
Station 1

You will find some toothpicks at this station. Use them to help you with this activity.

Here are several stages of a pattern made from toothpicks.

Stage 1  Stage 2  Stage 3

Work with other students to build the pattern from toothpicks.

Work together to answer the questions below. When everyone agrees on an answer, write it on the line.

1. How many toothpicks do you need to make Stage 4 and Stage 5?

________________________

2. Predict the number of toothpicks you would need to make Stage 10.

________________________

3. Explain how you made this prediction.

______________________________________________________________________
______________________________________________________________________
______________________________________________________________________

4. Write an expression that gives the number of toothpicks that are needed at Stage $x$.

________________________

5. Explain how you came up with the expression.

______________________________________________________________________
______________________________________________________________________
_____________________________________________________________________
Station 2

At this station, you will explore a pattern based on prices.

It costs $20 plus $35 per day to rent a car at Zippy Car Rentals.

Work with other students to complete the table.

<table>
<thead>
<tr>
<th>Number of days ((d))</th>
<th>1</th>
<th>3</th>
<th>5</th>
<th>8</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cost of car rental ((c))</td>
<td>$55</td>
<td>$125</td>
<td>$265</td>
<td></td>
</tr>
</tbody>
</table>

Work together to answer the questions below. When everyone agrees on an answer, write it on the line.

1. Write an expression that gives the cost of renting a car for \(d\) days.

   ______________________________________________________________________

2. Explain how you came up with the expression.

   ______________________________________________________________________
   ______________________________________________________________________
   ______________________________________________________________________

3. Show how you can use the expression to predict the cost of renting a car for 14 days.

   ______________________________________________________________________
   ______________________________________________________________________
   ______________________________________________________________________

4. Jerome rented a car at Zippy Car Rentals. The total cost was $335. For how many days did Jerome rent the car?

   ______________________________________________________________________

5. Explain how you found the answer to question 4.

   ______________________________________________________________________
   ______________________________________________________________________
   ______________________________________________________________________
Station 3

At this station, you will make your own table to help you explore a pattern.

A school bus can take 24 students on a field trip.

Work together to make a table that shows the number of buses and the corresponding number of students that can go on the field trip.

Work together to answer the questions below. When everyone agrees on an answer, write it on the line.

1. Write an expression that gives the number of student that can go on the field trip if there are \( b \) buses.

   _______________________

2. Explain how you came up with this expression.

   ___________________________________________________________
   ___________________________________________________________

3. Show how you can use the expression to find the number of students that can go on the trip if there are 12 buses.

   ___________________________________________________________
   ___________________________________________________________

4. How many buses are needed to take 216 students on the trip? Explain.

   ___________________________________________________________
   ___________________________________________________________
   ___________________________________________________________
Station 4

At this station, you will find some tiles that you may use to help you analyze a pattern.

Tessa is using circular stickers and square stickers to make a pattern. Here are the first three stages of her pattern.

Work together to answer these questions. When everyone agrees on an answer, write it on the lines below.

1. How many circular stickers will Tessa need for Stage 8? ________________________
   How many square stickers will she need for Stage 8? ________________________

2. Explain how you found the answers to the questions above.
   _______________________________________________________________________
   _______________________________________________________________________
   _______________________________________________________________________

3. Write an expression that gives the number of circular stickers at stage \( n \).
   __________________________________

4. Write an expression that gives the number of square stickers at stage \( n \).
   __________________________________

5. Write an expression that gives the total number of stickers at stage \( n \).
   __________________________________
The Number System

Set 1: Adding and Subtracting Rational Numbers

Goal: To provide opportunities for students to develop concepts and skills related to addition and subtraction

Common Core Standards

The Number System

Apply and extend previous understandings of operations with fractions to add, subtract, multiply, and divide rational numbers.

7.NS.1. Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram.

a. Describe situations in which opposite quantities combine to make 0.

b. Understand \( p + q \) as the number located a distance \(|q|\) from \( p \), in the positive or negative direction depending on whether \( q \) is positive or negative. Show that a number and its opposite have a sum of 0 (are additive inverses). Interpret sums of rational numbers by describing real-world contexts.

c. Understand subtraction of rational numbers as adding the additive inverse, \( p - q = p + (-q) \). Show that the distance between two rational numbers on the number line is the absolute value of their difference, and apply this principle in real-world contexts.

d. Apply properties of operations as strategies to add and subtract rational numbers.

Student Activities Overview and Answer Key

Station 1

Students model the sum of two integers using integer chips. They work as a group to ensure that the sum is modeled correctly. Then they use the model to find the sum of the integers.

Answers

1. \(-2\) 4. \(7\)
2. \(6\) 5. \(3\)
3. \(-8\) 6. \(0\)

Possible explanations: Count the remaining chips. If they are all yellow, the sum is the positive integer given by the number of remaining chips. If they are all red, the sum is the negative integer given by the number of remaining chips.
Station 2
Students are given a set of cards with integers written on them. They choose two cards at random and flip a coin to determine whether the two integers are to be added or subtracted. Students work together to find the sum or difference. When all students in the group agree on the answer, they write it down and repeat the process by choosing new integers to work with.

Answers
Answers will depend upon the numbers that are chosen.

Station 3
Students are given two sets of cards with rational numbers written on them. They choose one card from each set and work together to find the difference of the rational numbers. At the end of the activity, students discuss the strategies they used to subtract the numbers.

Answers
Answers will depend upon the cards that are chosen.
Possible strategies: If the cards show a decimal and a fraction, convert both numbers to decimals or both to fractions. If the number being subtracted is negative, change the problem to an addition problem. Model the subtraction problem with a number line.

Station 4
Students use a number cube to generate pairs of decimals. They work together to decide which of the two decimals in each pair is greater. Then they work together to subtract the smaller number from the larger one. All students in the group should agree on each answer.

Answers
Answers will depend upon the numbers that are rolled.
Possible strategies: Write the decimals so that one is above the other and so they are aligned on the decimal point. Add placeholder zeros if needed. Subtract the decimals as if they were whole numbers, placing the decimal in the answer in the same position as the decimals in the two given numbers.
The Number System
Set 1: Adding and Subtracting Rational Numbers

Materials List/Setup

Station 1  integer chips
Station 2  a penny
set of 8 index cards with the following numbers written on them:
−12, −9, −7, −3, 4, 6, 11, 12
Station 3  10 index cards, prepared as follows:
• set of 5 cards, labeled “A” on the back with the following rational numbers
  written on the front:
  −1⁄2, 2, −3, 4.5, −6.5
• set of 5 cards, labeled “B” on the back with the following rational numbers written
  on the front:
  0.5, −2, 4, 5 1⁄2, −7
• Place the cards face-down at the station, so that only the backs (A or B) are visible.
Station 4  number cube (numbers 1–6)
Discussion Guide

To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions

1. How do you add two integers with the same sign?
2. How do you add two integers with opposite signs?
3. What can you say about the sum of two numbers that are opposites, such as 3.5 and –3.5?
4. How do you use paper and pencil to add or subtract two decimals?

Think, Pair, Share

Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses

1. Add the absolute values of the integers. Use the same sign for the answer as the sign of the given integers.
2. Find the absolute value of the integers. Subtract the smaller absolute value from the greater absolute value. Use the sign of the integer with the greater absolute value.
3. The sum of the numbers is zero.
4. Write the decimals so that one is above the other and so they are aligned on the decimal point. Add zeros as placeholders if needed. Add or subtract the decimals as if they were whole numbers, placing the decimal in the answer in the same position as the decimals in the two given numbers.

Possible Misunderstandings/Mistakes

- Adding the absolute values of two integers when finding a sum of integers with opposite signs, rather than subtracting the absolute values (e.g., writing −3 + 2 = −5)
- Using the wrong sign for the sum or difference of integers (e.g., writing 8 + (−6) = −2)
- Not recognizing that opposite integers always have a sum of zero
Station 1

At this station, you will use integer chips to find the sum of two integers.

The yellow side of an integer chip shows +1. The red side shows –1. A pair of opposite chips (one yellow and one red) shows 0.

Work together using integer chips to show the first integer in each sum. Then use more integer chips to show the second integer in the sum. Work with other students to make sure each integer is shown correctly.

Then find the sum of the two integers by removing pairs of opposite chips and counting the chips that remain.

1. 5 + (–7) = ________

2. –2 + 8 = ________

3. –3 + (–5) = ________

4. –1 + 8 = ________

5. 7 + (–4) = ________

6. 6 + (–6) = ________

After removing the opposite pairs, how did you decide what integer was shown? Explain your method.

________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
Station 2

You will find a stack of cards and a penny at this station.

Choose two of the cards without looking. Turn the cards over and write the numbers in the boxes below. Then flip the penny. If it lands heads up, write “+” on the line between the numbers. If it lands tails up, write “–” on the line.

Answer: __________

Answer: __________

Answer: __________

Repeat the process three more times.
Station 3

You will be given two sets of cards labeled A and B. Choose one card labeled A and one card labeled B.

Turn the cards over. Subtract the rational number on card B from the rational number on card A. Write the subtraction problem below.

___________________

Work as a group to subtract the numbers. Everyone in the group should agree on your answer. Write the answer below.

___________________

Put the cards back. Mix up the cards. Repeat the process above three more times.

Subtraction problem: ___________________
Answer: ___________________

Subtraction problem: ___________________
Answer: ___________________

Subtraction problem: ___________________
Answer: ___________________

Subtraction problem: ___________________
Answer: ___________________

Explain the strategies you used to solve the subtraction problems.

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________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
Station 4

You will need a number cube for this activity. Use the number cube to create decimals.

Roll the number cube six times. Write the numbers in the six boxes below to create two decimals.

Work together to decide which of the two decimals is greater.

Subtract the smaller number from the larger one. Write the subtraction problem below.

Subtraction problem: ___________________

Work with other students to subtract the decimals. When everyone agrees on the answer, write it below.

Subtraction problem: ___________________

Repeat the process using the boxes below.

Subtraction problem: ___________________

Answer: ____________________

Explain the strategies you used to subtract the decimals.
The Number System

Set 2: Multiplying and Dividing Rational Numbers

Instruction

Goal: To provide students opportunities to develop concepts and skills related to multiplication and division

Common Core Standards

The Number System

Apply and extend previous understandings of operations with fractions to add, subtract, multiply, and divide rational numbers.

7.NS.2. Apply and extend previous understandings of multiplication and division and of fractions to multiply and divide rational numbers.

a. Understand that multiplication is extended from fractions to rational numbers by requiring that operations continue to satisfy the properties of operations, particularly the distributive property, leading to products such as \((-1)(-1) = 1\) and the rules for multiplying signed numbers. Interpret products of rational numbers by describing real-world contexts.

b. Understand that integers can be divided, provided that the divisor is not zero, and every quotient of integers (with non-zero divisor) is a rational number. If \(p\) and \(q\) are integers, then \(-\frac{p}{q} = \frac{-p}{q} = \frac{p}{-q}\). Interpret quotients of rational numbers by describing real-world contexts.

c. Apply properties of operations as strategies to multiply and divide rational numbers.

Student Activities Overview and Answer Key

Station 1

Students are given a set of cards with negative integers written on them. They choose two cards at random and flip a coin to determine whether the two integers are to be multiplied or divided. Students work together to find the product or quotient. When all students in the group agree on the answer, they write it down and repeat the process by choosing new integers to work with.

Answers

Answers will depend upon the numbers that are chosen.

Possible conclusion: All of the products and quotients are positive (i.e., the product or quotient of two negative numbers is positive).
Station 2

Students model the product of integers using integer chips. In each case, one integer in the product is positive and the other is negative. After working together to model a series of such products, students reflect on their work and write a statement about what they observe. In this way, students see that the product of a positive integer and a negative integer is always a negative integer.

Answers

\[-3 \times 5 = -15\]

1. \(-8\)  
2. \(-18\)  
3. \(-10\)

Possible conclusion: The product of a positive integer and a negative integer is always a negative integer.

Station 3

Students are given two sets of cards with positive and negative rational numbers written on them. They choose one card from each set and work together to find the quotient of the rational numbers. At the end of the activity, students discuss the strategies they used to divide the rational numbers.

Answers

Answers will depend upon the cards that are chosen.

Possible strategies: First convert mixed numbers to improper fractions. Convert decimals to fractions. Divide the fractions by changing the operation to multiplication and changing the divisor to its reciprocal. Then multiply and simplify the answer. Place the correct sign (+ or –) in front of the quotient.

Station 4

Students are given a set of ten cards with integers or expressions written on them. Students work together to find pairs of cards that show the same value. When all the cards have been paired, students work together to check that integers or expressions on the pairs of cards are equal.

Answers

1. \(-4 \times (-6) = 24; 8 \div (-2) = -4; -16 \times 2 = 4 \times (-8); -16 \div (-8) = -2 \times (-1); 6 \times (-4) = -48 \div 2\)

2. Possible strategies: First sort cards into two groups depending on whether the value shown on each card is positive or negative. Calculate products and quotients using the rules of integer arithmetic.
The Number System
Set 2: Multiplying and Dividing Rational Numbers

Materials List/Setup

Station 1  a penny
set of 8 index cards with the following numbers written on them:
-1, -2, -4, -6, -8, -12, -16, -32

Station 2  integer chips

Station 3  10 index cards, prepared as follows:
• set of 5 cards, labeled “A” on the back with the following rational numbers written on the front:
  -8, -20, 6 1/2, 8.5, -3 1/2
• set of 5 cards, labeled “B” on the back with the following rational numbers written on the front:
  1/2, 1/4, -0.5, -2, 4
• Place the cards face-down at the station, so that only the backs (A or B) are visible.

Station 4  10 index cards with the following numbers or expressions written on them:
-4 \times (-6), 24, 8 \div (-2), -4, -16 \times 2, 4 \times (-8), -16 \div (-8), -2 \times (-1), 6 \times (-4), -48 \div 2
The Number System
Set 2: Multiplying and Dividing Rational Numbers

Discussion Guide
To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions
1. What can you say about the product or quotient of two integers with the same sign?
2. What can you say about the product or quotient of two integers with opposite signs?
3. How is multiplication of integers like multiplication of whole numbers? How is it different?
4. How are multiplication and division of signed number similar to each other?

Think, Pair, Share
Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses
1. The product or quotient is positive.
2. The product or quotient is negative.
3. To multiply two integers, multiply their absolute values, which are whole numbers. The step that is different from multiplication of whole numbers is the final step in which you write the correct sign (positive if both numbers have the same sign, negative if the numbers have opposite signs).
4. The rules for determining the sign of the answer are the same. If the two numbers being multiplied or divided have the same sign, the answer is positive. If the signs are different, the answer is negative.

Possible Misunderstandings/Mistakes
• Writing an incorrect sign when multiplying or dividing integers (e.g., writing $-3 \times (-4) = -12$)
• Incorrectly converting mixed numbers to fractions
• Incorrectly converting decimals to fractions or vice versa
The Number System
Set 2: Multiplying and Dividing Rational Numbers

Station 1
You will find a stack of cards and a penny at this station.

Choose two of the cards without looking. Turn the cards over and write the numbers in the boxes below. Then flip the penny. If it lands heads up, write a multiplication sign (×) on the line between the numbers. If it lands tails up, write a division sign (÷) on the line.

Work with other students to solve the multiplication or division problem. When everyone agrees on the answer, write it below.

___________________

Repeat the process three more times.

Answer: ____________

Answer: ____________

Answer: ____________

What do you notice about all the products and quotients that you found?
_____________________________________________________________________
_____________________________________________________________________
_____________________________________________________________________
Station 2

In this activity, you will use integer chips to help you multiply integers. The yellow side of an integer chip shows +1. The red side shows −1.

To multiply −3 × 5, first use integer chips to show the negative number, −3. There are 5 groups of −3, so use additional chips to show that you have 5 groups of −3.

Work together to decide what integer is shown by all the chips. This is the product. Write it below.
___________________

Work with other students using integer chips to find each product.

1. −2 × 4 = ___________
2. 3 × (−6) = ___________
3. −5 × 2 = ___________
4. 7 × (−1) = ___________
5. −4 × 4 = ___________
6. −3 × 2 = ___________

Look at all the products you found. What can you say about the product of a positive integer and a negative integer?
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
Station 3

At this station, you will find two sets of cards labeled A and B. Choose one card labeled A and one card labeled B.

Turn the cards over. Divide the rational number on card A by the rational number on card B. Write the division problem below.

___________________

Work as a group to divide the rational numbers. Everyone in the group should agree on your answer. Write the answer below.

___________________

Put the cards back. Mix up the cards. Repeat the above process three more times.

Division problem: ___________________
Answer: ___________________

Division problem: ___________________
Answer: ___________________

Division problem: ___________________
Answer: ___________________

Explain at least three strategies that you could use to solve the division problems.
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
The Number System
Set 2: Multiplying and Dividing Rational Numbers

Station 4
At this station, you will find cards with the following numbers or expressions written on them:

\[-4 \times (-6) \quad 8 \div (-2) \quad 6 \times (-4) \quad 24 \quad -16 \times 2\]

\[-16 \div (-8) \quad -4 \quad 4 \times (-8) \quad -2 \times (-1) \quad -48 \div 2\]

Work with other students to sort the cards into pairs. The values on the two cards in each pair should be equal. When you have sorted the cards into pairs, work together to check that the values on the two cards in each pair are equal.

1. Write the five pairs below.

____________________________________________________________________
____________________________________________________________________
____________________________________________________________________
____________________________________________________________________
____________________________________________________________________

2. Describe the strategies you used to sort the cards into pairs.

____________________________________________________________________
____________________________________________________________________
____________________________________________________________________
____________________________________________________________________
____________________________________________________________________
The Number System

Set 3: Absolute Value

Goal: To provide opportunities for students to develop concepts and skills related to absolute values

Common Core Standards

The Number System

Apply and extend previous understandings of operations with fractions to add, subtract, multiply, and divide rational numbers.

7.NS.1. Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram.

a. Describe situations in which opposite quantities combine to make 0.

b. Understand $p + q$ as the number located a distance $|q|$ from $p$, in the positive or negative direction depending on whether $q$ is positive or negative. Show that a number and its opposite have a sum of 0 (are additive inverses). Interpret sums of rational numbers by describing real-world contexts.

c. Understand subtraction of rational numbers as adding the additive inverse, $p - q = p + (-q)$. Show that the distance between two rational numbers on the number line is the absolute value of their difference, and apply this principle in real-world contexts.

d. Apply properties of operations as strategies to add and subtract rational numbers.

7.NS.3. Solve real-world and mathematical problems involving the four operations with rational numbers.

Student Activities Overview and Answer Key

Station 1

Students work together to use a number line to plot numbers that have a given absolute value. Students reflect on their work to recognize that there are two points on a number line with a given absolute value (for positive absolute values) and one point (0) with an absolute value of zero.

Answers: 1. 1 and –1; 2. 3 and –3; 3. 4.5 and –4.5; 4. 0; 5. none

Possible responses: For a given positive absolute value, two points have the given absolute value. The only point with an absolute value of 0 is 0. No points have a negative absolute value.
Station 2
Students use a penny and a number cube to generate positive and negative two-digit numbers. They work together to find the absolute value of each of the numbers.

Answers: Answers will depend upon numbers that are rolled.

Possible explanation: If the number is positive, the absolute value of the number is the same as the number. If the number is negative, the absolute value of the number is the same as the number without its sign.

Station 3
Students are given a set of cards with positive and negative numbers written on them. Students work together to arrange the cards so that they are in order from the number with the least absolute value to the number with the greatest absolute value.

Answers: 0, –1, –1.5, 2, –3, 4.1, 8, –12

Possible strategies: First write the absolute value of each number. Then list the numbers so that the absolute values are listed in increasing order.

Station 4
Students are given a set of cards with numbers or expressions written on them. Students work together to form pairs of cards so that the numbers in each pair have the same absolute value. Then students reflect on the strategies they used to solve the problem.

Answers: 6 + 1 and –7; 5 and –5; 8 ÷ 4 and –2; 3 and 9 – 12; 2 + 8 and 2 – 12

Possible strategies: First simplify the expressions that involve operations. Look for pairs of numbers that are opposites.

Materials List/Setup
Station 1 none
Station 2 a penny; number cube (numbered 1–6)
Station 3 8 index cards with the following numbers written on them:
0, –1, –1.5, 2, –3, 4.1, 8, –12
Station 4 10 index cards with the following numbers or expressions written on them:
6 + 1, –7, 5, –5, 8 ÷ 4, –2, 3, 9 – 12, 2 + 8, 2 – 12
Discussion Guide

To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions

1. What is the absolute value of a number?
2. How do you find the absolute value of a number?
3. Can the absolute value of a number ever be negative? Why or why not?
4. Can two different numbers ever have the same absolute value? Explain.

Think, Pair, Share

Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses

1. the distance of the number from 0 on a number line
2. If the number is positive, the absolute value of the number is the same as the number. If the number is negative, the absolute value of the number is the same as the number without its sign. The absolute value of 0 is 0.
3. No. The absolute value represents a distance, so it cannot be negative.
4. Yes. A number and its opposite, such as 5 and –5, have the same absolute value.

Possible Misunderstandings/Mistakes

- Forgetting that the absolute value of a number cannot be negative
- Incorrectly finding the absolute value of expressions (e.g., thinking |2 – 12| = |2| – |12|)
- Incorrectly ordering the absolute value of two numbers (e.g., stating that |–5| is less than |4| because –5 is less than 4)
Station 1

In this activity, you will work with other students to plot points on a number line. Recall that the absolute value of a number is its distance from zero on a number line.

For each of the following, plot all the points (if any) that satisfy the statement.

1. The absolute value is 1.

2. The absolute value is 3.

3. The absolute value is 4.5.

4. The absolute value is 0.

5. The absolute value is –2.

Work with other students to list at least three things you notice from your work.
Station 2
You will find a penny and a number cube at this station. You will use these to create positive and negative numbers.

Flip the penny. If it lands heads up, write “+” on the line below. If it lands tails up, write “–” on the line. Then roll the number cube two times. Write the numbers in the two boxes below.

__________________  __________________

Find the absolute value of the number. ________

Repeat the process four more times.

__________________  __________________  __________________  __________________

Absolute value: ________  Absolute value: ________

__________________  __________________  __________________  __________________

Absolute value: ________  Absolute value: ________

Explain how you found the absolute values of the numbers.

________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
Station 3
You will find a set of cards at this station. The cards have the following numbers written on them.

\[-1.5 \quad 4.1 \quad 0 \quad -12 \quad 8 \quad -1 \quad -3 \quad 2\]

Work with other students to arrange the cards so that they are in order from the number with the least absolute value to the number with the greatest absolute value.

Write your answer below.

__________________________________________________________________________

Work together to check that the numbers are in the correct order.

Describe the strategies you used to solve this problem.

__________________________________________________________________________

__________________________________________________________________________

__________________________________________________________________________
Station 4

You will be given a set of index cards with the following numbers and expressions on them:

\[
\begin{array}{cccccc}
6 + 1 & 5 & 9 - 12 & -2 & -7 \\
-5 & 2 - 12 & 3 & 8 ÷ 4 & 2 + 8
\end{array}
\]

Work with other students to form pairs of cards. The two numbers or expressions in each pair should have the same absolute value.

Work together to check that the numbers or expressions in each pair have the same absolute value. Write the pairs below.

____________________
____________________
____________________
____________________
____________________

Describe any strategies you used to solve this problem.

________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
Goal: To provide opportunities for students to develop concepts and skills related to simplifying algebraic expressions, solving linear equations in one variable, and solving multi-step linear equations and inequalities. Students will also identify and apply properties of real numbers and equality.

Common Core Standards
Expressions and Equations
Use properties of operations to generate equivalent expressions.

7.EE.1. Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients.

7.EE.2. Understand that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related.

Solve real-life and mathematical problems using numerical and algebraic expressions and equations.

Student Activities Overview and Answer Key
Station 1
Students will be given four index cards that contain equations and fifteen index cards that contain the “steps” required to solve the equations. Students work as a group to place “step” cards sequentially with the appropriate equation, ending in the solution.

Answers
Order of equation cards will vary. Check to ensure steps are grouped in the following order with their respective equations:

Equation: \(3x + 2 - x = -\frac{2}{3}x + 26\)
Step cards:
\[\begin{align*}
2x + 2 &= -\frac{2}{3}x + 26 \\
\frac{8}{3}x + 2 &= 26 \\
\frac{8}{3}x &= 24 \\
x &= 9
\end{align*}\]

Equation: \(\frac{x}{2} = \frac{x}{4} + 12\)
Step cards:
\[\begin{align*}
\frac{x}{2} - \frac{x}{4} &= 12 \\
\frac{2x}{4} - \frac{x}{4} &= 12 \\
\frac{x}{4} &= 12 \\
x &= 48
\end{align*}\]
Expressions and Equations
Set 1: Solving Linear Equations

Instruction

Equation: \(10x - 5 = 5x + 20\)

Step cards:

\(5x - 5 = 20\)
\(5x = 25\)
\(x = 5\)

Equation: \(2(x + 4) = \frac{2}{3}(x - 24)\)

Step cards:

\(2x + 8 = \frac{2}{3}x - 16\)
\(\frac{4}{3}x + 8 = -16\)
\(\frac{4}{3}x = -24\)
\(x = -18\)

Station 2

Students will be given eight index cards with the following final simplified algebraic expressions written on them: \(4x + 2, 3b - 10, \frac{5}{8} y - 12, \frac{-3}{7} c + \frac{4}{9}, -x, 6xy^3, \frac{2x}{3z^2}, a^3b^2\). Students shuffle and place the index cards in a pile. One student draws a card and they work as a group to create an algebraic expression that precedes this simplified expression. Then they simplify given algebraic expressions.

Answers

1. Answers will vary. Possible answers include:

\[2x + 2x + 2; 10b - 7b - 5 - 5; \frac{3}{8} y + \frac{1}{4} y - 12; \frac{-3}{7} c + \frac{2}{9} + \frac{2}{9}; 5x - 6x; 2xy \cdot 3y^2; \frac{x}{3z} \cdot \frac{2}{z}; a^2b \cdot ab\]

2a. \(-4x + 15\)

2b. \(8x^2y + 72y - 3\)

2c. \(14x^3 + 3xy^2 + 12x^2 - 21x\)

2d. \(-\frac{1}{4} x + 4\)
Station 3

Students will be given a number cube. They roll the number cube to populate boxes that will represent the commutative and associative properties. They will derive the commutative and associative properties based on their observations. Students will realize that these properties only work for addition and multiplication. They will derive the distributive property based on an example.

Answers

1. Answers will vary; yes; commutative property is when you change the order of the numbers without changing the result; just addition and multiplication. Subtraction and division won’t give you the same answer.

2. Answers will vary; no, because they are addition and multiplication; associative property is when you change the grouping of the numbers without changing the result; just addition and multiplication. Subtraction and division won’t give you the same answer.

3. Distributive property is when a number is multiplied by the sum of two other numbers; the first number can be distributed to both of those two numbers and multiplied by each of them separately.

4. a. $10x + 2y$; distributive; b. commutative; c. no, because it is subtraction; d. associative; e. no, because it is division.

5. Answers will vary. Possible answers include: Figuring out the cost of a movie based on the number of people in two families that are going to the movie. $C(F_1 + F_2)$, for which $C =$ cost of movie, $F_1 =$ number of people in family 1, and $F_2 =$ number of people in family 2.

Station 4

Students will work together to write and solve linear equations based on real-world examples. They will provide the equation and the solution.

Answers

1. $45 + 0.25x = 145; x = 400$ minutes

2. $125 + 4x = 157; x = $8 per can

3. $20 + 10x \leq 100; x \leq 8; $ no more than 8 yoga classes per month

4. $x(16 - 2) \geq 210; x \geq 15; $ no fewer than 15 DVDs per month
Expressions and Equations
Set 1: Solving Linear Equations

Materials List/Setup

Station 1

Four index cards with the following equations written on them:

\[
3x + 2 - x = - \frac{2}{3} x + 26, \quad 10x - 5 = 5x + 20, \quad \frac{x}{2} = \frac{x}{4} + 12, \quad 2(x + 4) = \frac{2}{3}(x - 24)
\]

Fifteen index cards with the following “steps” written on them:

\[
\begin{align*}
2x + 2 &= - \frac{2}{3} x + 26 \\
5x - 5 &= 20 \\
\frac{8}{3} x + 2 &= 26 \\
5x &= 25 \\
\frac{8}{3} x &= 24 \\
x &= 9 \\
\frac{8}{x} &= 12 \\
\frac{4}{4} &= 4 \\
\frac{x}{x} &= 12 \\
\frac{x}{4} &= 3 \\
x &= 48 \\
x &= 18
\end{align*}
\]

Station 2

Eight index cards with the following final simplified algebraic expressions written on them:

\[
4x + 2, \quad 3b - 10, \quad \frac{5}{8} y - 12, \quad \frac{-3}{9} c + \frac{4}{7} x, \quad 6xy^2, \quad \frac{2x}{3z^2}, \quad a^2b^2
\]

Station 3

Number cube

Station 4

None
Expressions and Equations
Set 1: Solving Linear Equations

Discussion Guide
To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions
1. How do you solve linear equations?
2. How do you simplify algebraic expressions?
3. What is the commutative property?
4. What is the associative property?
5. What is the distributive property?
6. What are examples of real-world applications of linear equations?

Think, Pair, Share
Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses
1. Combine like terms if necessary. Use the properties of equality to get the variable by itself on one side of the equation. Solve for the variable by making its coefficient equal to 1.
2. Combine like terms and use the order of operations.
3. The commutative property is when you change the order of the numbers without changing the result.
4. The associative property is when you change the grouping of the numbers without changing the result.
5. The distributive property is when a number is multiplied by the sum of two other numbers; the first number can be distributed to both of those two numbers and multiplied by each of them separately.
6. Answers will vary. Possible answers include: the cost of services (including water, telephone, and electricity) based on a flat rate plus a usage fee.
Expressions and Equations
Set 1: Solving Linear Equations

Possible Misunderstandings/Mistakes

- Incorrectly identifying subtraction and division problems as depicting commutative or associative properties
- Incorrectly identifying the constant versus the coefficient of the variable when writing and solving linear equations and inequalities
- Using the wrong sign (i.e., < instead of >) when writing and solving inequalities
- Simplifying algebraic expressions by combining unlike terms
Station 1
You will be given four index cards with equations written on them. You will also be given fifteen index cards with steps for solving the equations written on them. Place the “equation” cards in one pile and lay out the “step” cards on your table or desk. Draw a card from the equation deck. Find all the step cards that show the steps for solving that equation. Place them in order underneath the equation, ending with the solution as the last step. Repeat the process for each equation card.

On the lines below, write the equation, the steps to solve it in order, and the corresponding last step (the solution).

Equation 1: ____________________  Equation 3: ____________________
______________________
______________________
______________________
______________________
______________________

Equation 2: ____________________  Equation 4: ____________________
______________________
______________________
______________________
______________________
______________________
Station 2
You will be given eight index cards with the following final simplified algebraic expressions written on them:

\[ 4x + 2, \ 3b - 10, \ \frac{5}{8}y - 12, \ -\frac{3}{7}c + \frac{4}{9}, \ -x, \ 6xy^3, \ \frac{2x}{3z^2}, \ a^2b^2 \]

Shuffle and place the index cards in a pile. Have one student draw a card. As a group, create an algebraic expression that precedes this simplified expression. For example, if you had drawn a card that read \(3x - 15\), then your answer could be \(7x - 4x - 15\) or \(8x - 10 - 5x - 5\), etc.

1. As a group, come to an agreement on your answers. Write the final algebraic expression and your answers on the lines below.

_____________________________________________________________________
_____________________________________________________________________
_____________________________________________________________________
_____________________________________________________________________
_____________________________________________________________________
_____________________________________________________________________
_____________________________________________________________________

2. As a group, simplify the following algebraic expressions:

a. \(-x + 14 - 3x + 1 = \) ________________

b. \(8y(x^2 + 9) - 3 = \) ________________

c. \(12x^2 - 19x + 4xy^2 + 14x^3 - 2x - xy^2 = \) ________________

d. \(\frac{1}{2}x + 4 - \frac{3}{4}x = \) ________________
Expressions and Equations
Set 1: Solving Linear Equations

Station 3
Use the number cube provided to complete and solve the problems below.

1. As a group, roll the number cube and write the result in the first box. Roll again, then write the second number in the second box for each problem. Then find the sum and product.

\[ s + s = \]
\[ a \times a = \]

If you add or multiply the terms in reverse order, do you get the same answers? __________
This problem represents the commutative property. Write a definition of the commutative property based on your observations.

Does the commutative property hold for addition, subtraction, multiplication, and division? Why or why not?

2. As a group, roll the number cube and write the result in the first box. Repeat this process to write a number in the second and third boxes for each problem. Then write the same three numbers in the same order in the last three boxes for each problem.

\[ z + (z + z) = (z + z) + z = \]
\[ a \times (b \times b) = (a \times b) \times b = \]
Does the grouping of the terms, as shown by the parentheses, change the answer on each side of the equation? Why or why not?

This problem represents the associative property. Write a definition of the associative property based on your observations.

Does the associative property hold for addition, subtraction, multiplication, and division? Why or why not?

3. The following problem depicts the distributive property:
\[4x(7 + 9) = 4x(7) + 4x(9) = 28x + 36x = 64x\]

Based on this problem, write a definition for the distributive property in the lines below.

4. For each problem below, identify the property used as commutative, associative, or distributive. Simplify the problem if necessary. If the problem doesn’t represent one of these properties, explain why.
   a. \[2(5x + y) = \]
   b. \[34 + 12x + 10 = 10 + 34 + 12x\]
Expressions and Equations
Set 1: Solving Linear Equations

c. \(12x^2 - 5x^2 = 5x^2 - 12x^2\)

d. \((1a + 16a) + 29a = 1a + (16a + 29a)\)

e. \(24x^2 + 3y = 3y + 24x^2\)

5. What is one real-world example of when you would use the distributive property?
Station 4

Write equations for real-world situations and then solve the equations. Work with your group to write and solve the equations. When everyone agrees on the correct equation and solution, write them in the space provided.

1. Janice needs to figure out her cell phone bill. She is charged a monthly flat fee of $45. She is also charged $0.25 per minute. How many minutes did she use if her cell phone bill was $145?

   Equation: ___________________  Solution: ___________________

2. Manny spent $157 at a sporting goods store. He bought a warm-up suit for $125 and spent the rest of the money on cans of tennis balls. If each can of tennis balls costs $4, how many cans did he buy?

   Equation: ___________________  Solution: ___________________

Now you will write inequalities for real-world situations and then solve the inequalities. Work with your group to write and solve the inequalities.

3. Megan joined a gym for a monthly fee of $20. She has a budget of no more than $100 per month. She wants to take yoga classes that cost $10. How many yoga classes can she take each month and stay within her budget?

   Inequality: ___________________  Solution: ___________________

4. John sells DVDs on the Internet. He wants to make no less than $210 per month. He sells the DVDs for $16, and it costs him $2 to ship each DVD. How many DVDs must he sell to make no less than $210 per month?

   Inequality: ___________________  Solution: ___________________
Goal: To provide students the opportunity to apply problem-solving skills and knowledge of rational numbers in any form, properties of operations, and converting between forms

Common Core Standards
Solve real-life and mathematical problems using numerical and algebraic expressions and equations.

7.EE.3. Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.

Student Activities Overview and Answer Key

Station 1
Students will work together to calculate a pay increase for a burger joint employee, including hourly increase, new hourly wage, expected earnings for a 12-hour week, and difference in earnings before and after the raise.

Answers
1. 78 cents
2. $8.58
3. $102.96
4. $9.36

Station 2
Students will work together to determine how much of a raise or how many additional hours of babysitting would be necessary to earn a certain amount of money in a certain amount of time.

Answers
1. $195
2. $55
3. 8.5 to 9 hours
4. He would need to charge $1.83 more per hour.
5. Answers will vary, but should add up to at least $250.
Expressions and Equations
Set 2: Multi-Step Real-Life Problems with Rational Numbers

Station 3
Students will work together to determine how to place two posters on a bedroom wall, with even spacing on either side and between the two posters.

Answers
1. 50 inches
2. inches; 104 inches
3. 18 inches on either side and between
4. Answers will vary, but must add up to a total of 104 inches.
5. Diagrams should show two 25-inch wide posters spaced 18 inches apart with 18 inches of space on either side on a 104-inch-wide wall (8 2⁄3 feet). Check diagram labels for accuracy.

Station 4
Students will work together to figure out what size containers to use to store lemonade. They will need to calculate the number of cups of lemonade needed for a party and what combination of containers will hold the lemonade.

Answers
1. 14 cups
2. 3.5 quarts
3. four 1-quart pitchers
4. 0.875 gallons
5. 1 gallon pitcher
6. Answers will vary, but should account for 14 cups of lemonade and should provide an explanation. For example, “One gallon pitcher is a better choice because then you only need one.” OR “Four quart pitchers are better because they are easier to pour and everyone will have one nearby.”

Materials List/Setup
Station 1 optional: calculators
Station 2 optional: calculators
Station 3 optional: calculators; tape measure
Station 4 optional: calculators; water; separate containers to hold 1 cup, 1 quart, and 1 gallon of water, respectively
Expressions and Equations
Set 2: Multi-Step Real-Life Problems with Rational Numbers

Discussion Guide
To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions
1. How do you calculate a raise or other increase (in price, temperature, etc.)? What are the steps?
2. How do you work backward from an amount of money that you want or need in order to figure out how to earn/save it?
3. How do you convert between measurements such as from inches to feet, feet to yards, cups to quarts, quarts to gallons?
4. In a multi-step problem, how do you know if your answer is correct?

Think, Pair, Share
Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses
1. Multiply by the percent or fraction increase and then add to the original rate/price/temperature.
2. Divide the total amount by the hourly/daily/weekly rate. If appropriate, first subtract the existing amount.
3. Remember, or look up the conversions—12 inches per foot and 3 feet per yard; 4 cups per quart and 4 quarts per gallon.
4. Substitute your solution back into the problem to see if it works. Do a “common sense” check to make sure it’s reasonable.

Possible Misunderstandings/Mistakes
- Difficulty converting a fraction or percent to value in dollars and cents
- Forgetting one or more steps in a multi-step problem; e.g., failing to add or subtract from the original amount
- Making errors in converting amongst units of measure, or using incorrect equivalents
- Not using the scenario provided to help reason through the mathematics
Station 1

Jayda works at a burger restaurant. She gets paid $7.80 per hour. Now that she’s worked part-time for six months, she is getting a 10-percent raise!

Use the information in the problem to answer each question. Show and explain your math.

1. What is a 10-percent raise on $7.80 per hour?

2. How much will Jayda make per hour after her raise?

3. How much will Jayda earn in a week if she works for 12 hours at her new wage?

4. How much more will she be making this week than she did last week (if both are 12-hour work weeks)?
Station 2

Damian plans to do a lot of babysitting this summer. He charges $6.50 per hour and usually babysits for 3 hours. He has agreed to babysit every Saturday from mid-June through August (10 times) for his neighbors.

Damian’s parents said that they would split the cost of a new computer with him. It costs $500 and he has to save half that amount before school starts.

Use the information in the problem to answer each question. Show and explain your math.

1. How much money will Damian earn from the babysitting that he already has scheduled?

2. How much more money will he need to make a total of $250?

3. How many more hours will he have to babysit to earn the extra money that he needs?

4. How much more would Damian have to charge per hour if he wanted to make the whole $250, in the number of hours he already has scheduled to babysit?

5. If Damian wants to do a combination of raising his prices and working more hours, would that work? How could he do it and raise the $250 he needs?
Station 3

Mike’s brother is going to college, so now he has a bedroom to himself. Mike wants to put up 2 new movie posters on the wall that used to be his brother’s. The wall is $8 \frac{2}{3}$ feet wide and each poster is 25 inches wide. He wants the posters spaced out so there is the same amount of space on either side of the posters, and between them, too.

Use the information in the problem to answer each question. Show and explain your math. Then, make a diagram of the wall and the 2 posters and label the measurements.

1. How wide are the 2 posters together?

2. What unit of measurement will you have to use for the width of the wall? How wide is the wall in this unit of measurement?

3. How much space will there be between the posters and on either side, if they are spaced evenly?
4. How else could you space the posters on the wall? List the distances on either side and between them.

5. Draw a diagram of the wall showing how Mike arranged the posters. Label the measurements for the posters and the space on either side and between them.
Station 4

Holly and Aubrey are having a party. They plan to serve lemonade. Including the two girls, there will be 14 guests at the party. Holly and Aubrey are assuming that each person will have a cup of lemonade.

Use the information in the problem to answer each question. You may also use cups, pitchers, and water if your teacher provides them. Show and explain your math.

1. How many cups of lemonade do Holly and Aubrey need for their party?

2. How many quarts of lemonade is that?

3. How many quart pitchers would Holly and Aubrey need to store and serve the lemonade?

4. How many gallons of lemonade do the number of cups equal?

5. How many gallon pitchers would Holly and Aubrey need to store and serve the lemonade?

6. Which is the better size pitcher to use—quart or gallon? Explain your reasoning.
Expressions and Equations
Set 3: Using Variables to Construct Equations and Inequalities

Goal: To provide students opportunities to interpret word problems and to construct simple equations and expressions to solve them

Common Core Standards
Solve real-life and mathematical problems using numerical and algebraic expressions and equations.

7.EE.4. Use variables to represent quantities in a real-world or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities.

a. Solve word problems leading to equations of the form $px + q = r$ and $p(x + q) = r$, where $p$, $q$, and $r$ are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach.

b. Solve word problems leading to inequalities of the form $px + q > r$ or $px + q < r$, where $p$, $q$, and $r$ are specific rational numbers. Graph the solution set of the inequality and interpret it in the context of the problem.

Student Activities Overview and Answer Key
Station 1
Students will write an equation, using variables, to represent the length, width, and perimeter of a dance floor. They will solve for width, given side length and perimeter. They will then write an equation for the area of the dance floor and solve using the information that they already have.

Answers
1. $2l + 2w = p$
2. $2(20) + 2w = 60$
   $40 + 2w = 60$
   $2w = 20$
   $w = 10$
3. $l \cdot w = a$ or $20 \cdot 10 = a$
4. $20 \cdot 10 = 200 \text{ m}^2$
Expressions and Equations
Set 3: Using Variables to Construct Equations and Inequalities

Station 2
Students will write an inequality, using variables, to represent the number of times Mia will have to watch her little brother, in addition to her regular allowance, to save $25 this week.

Answers
1. $10 + 3x \geq 25$
2. $x \geq 5; Mia must watch her brother for 5 or more hours.

Station 3
Students will write two different forms of an equation, using variables, to represent the total number of lemonade sales two boys made in order to make $2.40. Students will then list at least three combinations that add up to the necessary total.

Answers
1. $0.50R + 0.50A = T$, or $0.50(R + A) = T$
2. 48 cups of lemonade
3. Answers will vary, but should sum to 48.

Station 4
Students will write an inequality, using variables, to represent the number of magazine subscriptions they need to sell in order to reach or exceed their goal. Then they describe the solution to the inequality.

Answers
1. $150 + 5x \geq 500$
2. $x \geq 70; they have to sell at least 70 more subscriptions.

Materials List/Setup
Station 1 calculators and scrap/scratch paper
Station 2 calculators and scrap/scratch paper
Station 3 calculators and scrap/scratch paper
Station 4 calculators and scrap/scratch paper
Discussion Guide

To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions

1. What is a variable?
2. How do you decide what values need to be represented by a variable?
3. What is the difference between an equation and an inequality?
4. Why is it important to label answers?

Think, Pair, Share

Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses

1. A variable is a letter used to represent an unknown value.
2. When writing an equation or inequality, you need to use a variable to represent each value that you don’t know.
3. An equation has a finite number of answers. An inequality has a range (infinite number) of correct answers.
4. Units or labels make it clear what the answer actually represents. (Dollars? Inches? Subscriptions?)

Possible Misunderstandings/Mistakes

- Difficulty identifying which values need to be represented with a variable
- Difficulty selecting/assigning a variable (Point out that there is no “rule;” x, y, z are common; and using initials such as s for subscriptions, is helpful.)
- Lacking knowledge of standard formulas for perimeter, area, etc.
- Confusion about the difference between an equation and an inequality
- Confusion about ≤ versus ≥ in a given situation
- Failing to label answers
- Failing to understand what solutions represent vis-à-vis the problem
Station 1

A dance floor has a perimeter of 60 meters. The dance floor is 20 meters long. Use this information to help you follow the directions below.

1. Write an equation using variables to represent the perimeter of the dance floor.

2. Solve the equation to find the dimensions of the dance floor.

3. Write an equation using variables to represent the area of the dance floor.

4. Solve the equation to find the area of the dance floor.
Station 2

Mia’s mother gives her $10 per week for allowance. Mia gets an additional $3 for every hour she spends watching her little brother. Mia wants to make at least $25 this week to spend shopping with her friends. Use this information to help you follow the directions below.

1. Write an inequality, using variables, to represent the number of times that Mia has to watch her brother in order to get at least $25.

2. Solve your inequality and describe the solution.
Station 3

Raf and Ali set up two lemonade stands in their neighborhood. They each charge $0.50 for a cup of lemonade. At the end of the day, they meet to combine their earnings. Use this information to help you follow the directions below.

1. Write two different equations, using variables, to represent the amount of money that the boys will make.

2. Together, Raf and Ali got $24.00. How many cups did they sell?

3. Show at least three different combinations of lemonade sales for Raf and Ali that would add up to earnings of $24.00.
Station 4

Ms. Mohammed’s class is selling magazine subscriptions to earn money for a field trip. For every subscription sold, the class makes $5. They have already earned $150, but they need $500 total. Use this information to help you follow the directions and answer the questions below.

1. Write an inequality, using variables, to represent the number of subscriptions that will have to be sold to make at least $500.

2. Solve the inequality and describe the solution. How many more subscriptions does Ms. Mohammed’s class have to sell?
Geometry

Set 1: Constructing Plane Figures

Goal: To provide opportunities for students to develop concepts and skills related to basic construction of segments, angles, triangles, and so forth

Common Core Standards

Geometry

Draw, construct, and describe geometrical figures and describe the relationships between them.

7.G.2. Draw (freehand, with ruler and protractor, and with technology) geometric shapes with given conditions. Focus on constructing triangles from three measures of angles or sides, noticing when the conditions determine a unique triangle, more than one triangle, or no triangle.

Student Activities Overview and Answer Key

Station 1

Students will explore how congruent triangles make up many of the figures we talk about. They do this though rearranging congruent triangles and observing what happens. They then think about other polygons and how congruent triangles are important.

Answers: Answers will vary (trapezoid, parallelogram, triangle, etc.); it increases by the area of one triangle each time; start with the middle point and draw eight segments to the vertices

Station 2

At this station, students use a compass and ruler to construct a perpendicular line. They follow a series of instructions and then use a protractor to verify their finding.

Answers: 90 degrees; 90 degrees; They are perpendicular.

Station 3

Students use a compass and ruler to construct an angle bisector. They follow directions and use a protractor to determine that the angle is bisected.

Answers: Answers will vary; answers will vary; they are equal; an angle bisector
Station 4

Students use a compass and ruler to construct an angle that is congruent to a given angle. They follow a set of instructions, use a protractor to measure the two angles, and discover that they are equal in measure.

Answers: Answers will vary; answers will vary; They are congruent.

Materials List/Setup

Station 1 a ruler; a set of at least 5 congruent triangles
Station 2 enough compasses, protractors, and rulers for all group members
Station 3 enough compasses, protractors, and rulers for all group members
Station 4 enough compasses, protractors, and rulers for all group members
Discussion Guide

To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions

1. How could you use our method of constructing a perpendicular line to construct a line parallel to a given line?
2. Can you think of another figure that is made up of congruent triangles? What?
3. If you had an angle that was 60 degrees, how could you use a compass and ruler to construct an equilateral triangle?
4. How is constructing a perpendicular line like constructing an angle bisector?

Think, Pair, Share

Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses

1. make a line that is perpendicular to our perpendicular line
2. any regular polygon
3. copy the angle twice so you have three 60° angles, and connect them
4. A perpendicular line is an angle bisector for a straight angle. They are constructed in a similar way.

Possible Misunderstandings/Mistakes

- Having trouble keeping the compass open at a constant angle
- Having difficulty measuring angles
- Not coming up with all the possible shapes at Station 1
Geometry
Set 1: Constructing Plane Figures

Station 1

At this station, you will find a set of congruent triangles and a ruler. You will use these triangles to make new shapes.

Work with your group members to rearrange the triangles. Make as many shapes as possible using these triangles (e.g., parallelogram, trapezoid, etc.). Record your findings in the table below.

<table>
<thead>
<tr>
<th>Number of congruent triangles</th>
<th>Possible shapes</th>
<th>Total area</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td></td>
<td></td>
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<tr>
<td>2</td>
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<td>5</td>
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</tbody>
</table>

How many different shapes did you develop? ____________________

What do you notice about the total area? __________________________________________

______________________________________________________________________________

Think about a regular octagon. Can you find the congruent triangles that make up an octagon?
Station 2
At this station, you will find enough protractors, compasses, and rulers for everyone. Each of you should follow the directions on your own sheet.

Using the ruler, draw a line in the space below. Place a point, A, on the line.

Now, using the compass, draw two arcs through the line. Your compass must be centered at point A and the arcs must both be the same distance from A. Label these points B and C.

Open your compass a little more. Center it at point B. Make an arc in the area above point A. Repeat this step with the center at point C and the same radius that was used with point B. These two arcs should intersect. Call this point D.

Using the ruler, draw a segment from the intersection to your line.

Measure angles DAB and DAC.

Measure of angle DAB =

Measure of angle DAC =

Compare your answers and discuss what you notice about segments DA and BC. Explain below.
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
Station 3

At this station, you will find enough protractors, compasses, and rulers for everyone. Each of you should follow the directions on your own sheet.

Using a ruler, draw an angle in the space below. This can be any angle you would like, but make sure it is large enough for you to draw between the two rays.

Center your compass at the vertex of the angle, point A. Make an arc that goes through both rays of the angle. Call one of the intersections B and the other C.

Now center your compass at point B. Draw an arc between the two rays. Repeat this step with point C, being sure to use the same radius. Call this new intersection point D. Draw a segment from A to D.

Measure angles BAD and DAC.

Measure of angle BAD =

Measure of angle DAC =

Compare your work with your group. What do you notice?

________________________________________________________________________

________________________________________________________________________

What do we call line segment AD?____________________
Station 4

At this station, you will find enough protractors, compasses, and rulers for everyone.

With your ruler, draw an angle (vertex $A$) in the space below.

Draw a ray next to that angle. Using your compass, draw an arc that intersects both rays in the original angle. Label the two intersections $B$ and $C$.

Keep your compass to the same radius and center the compass at the endpoint of the ray you created. Draw an arc that intersects the ray and continues well past it in both directions. Label the intersection point $E$.

Go back to the original angle. Open the compass so that it is centered on point $C$ and also touches point $B$. In other words, the radius should be equal to the distance from $B$ to $C$.

Being careful to keep this radius, center your compass on point $E$. Draw an arc such that it intersects the other arc.

Using your ruler, draw a line segment from this point of intersection back to the endpoint of the ray, forming an angle.

Measure the original angle. What is its measure? _________________

Measure the angle you constructed. What is its measure? _________________

Discuss your work with others in your group. What do you notice?

__________________________________________________________________________

__________________________________________________________________________
Geometry

Set 2: Similarity and Scale

Instruction

Goal: To provide opportunities for students to develop concepts and skills related to the properties of similarity

Common Core Standards

Geometry

Draw, construct, and describe geometrical figures and describe the relationships between them.

7.G.1. Solve problems involving scale drawings of geometric figures, including computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale.

7.G.2. Draw (freehand, with ruler and protractor, and with technology) geometric shapes with given conditions. Focus on constructing triangles from three measures of angles or sides, noticing when the conditions determine a unique triangle, more than one triangle, or no triangle.

Student Activities Overview and Answer Key

Station 1

At this station, students draw different triangles with the same three angles. They then measure their sides and compare the ratios of the sides. Students reflect on their findings.

Answers: The ratios are approximately the same for all the triangles; they are similar; the ratio of the sides in similar triangles is the same

Station 2

Students imagine they are architects. They use a scale diagram of a room to determine the actual measurements of a room.

Answers: They are similar; it is useful to share plans with other people; they cannot possibly make their plans the same size as what they are building, etc.

Station 3

Students look at a model car. They take measurements and use scale factor to determine the measurements of the actual car. They then reflect on the relationship between the model car and the actual car.

Answers: All measurements vary; similar because all the measurements of the model car are proportional to the actual car, but not exact
Station 4

Students explore the relationship between similarity and area in triangles. They construct their own triangles and find the ratio of the areas. They then reflect on their observations.

**Answers:** 6 sq in.; 24 sq in.; 4 to 1; answers will vary; answers will vary; 4 to 1; the ratio is 4 to 1; the base and height are both increased by a factor of 2, and \(2 \times 2\) is 4

**Materials List/Setup**

- **Station 1** enough pencils, protractors, rulers, and calculators for all group members
- **Station 2** enough rulers and calculators for all group members
- **Station 3** a model car with scale factor; enough rulers and calculators for all group members
- **Station 4** enough rulers and calculators for all group members
Geometry
Set 2: Similarity and Scale

Discussion Guide
To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions
1. How are similarity and congruence different?
2. When is scale factor important in real life?
3. What is the ratio of a large rectangle’s area to a small rectangle’s area if the dimensions are increased by a factor of 2?
4. If you had a figure and wanted to construct a similar figure, what information would be important to know?

Think, Pair, Share
Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses
1. Similar figures have the same angles. Congruent figures have the same angles and sides.
2. many possibilities—in blueprints
3. 4 to 1
4. the angles, proportions of the sides

Possible Misunderstandings/Mistakes
- Trouble accurately measuring angles—if incorrect, data and lesson will be incorrect
- Trouble accurately using a ruler to measure sides—if incorrect, data and lesson will be incorrect
- Confusing units when dealing with scale factor
Station 1

At this station, you will find rulers, pencils, calculators, and protractors. You will be using these materials to draw a triangle and make observations.

Each group member should draw a triangle in the space below. The angles of the triangle should be 82°, 28°, and 70°. The 82° angle is angle $A$. The 28° angle is angle $B$. And the 70° angle is angle $C$.

Each person should measure the sides of his/her triangle. Compile your data in the table below.

<table>
<thead>
<tr>
<th>Group member</th>
<th>Length $AB$ (cm)</th>
<th>Length $BC$ (cm)</th>
<th>Length $AC$ (cm)</th>
<th>$AB/BC$</th>
<th>$BC/AC$</th>
<th>$AB/AC$</th>
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</tbody>
</table>
What do you notice about the ratio of the sides? ______________________________________
__________________________________________________________________________
__________________________________________________________________________

What types of triangles are these? What is the relationship between any two of the triangles?
__________________________________________________________________________
__________________________________________________________________________

What do you notice about similar triangles?________________________________________
__________________________________________________________________________
__________________________________________________________________________
Station 2

At this station, you will take on the role of an architect. You will find rulers and calculators to help you with this role.

Below is a diagram of a room in a house. Work as a group to figure out the dimensions of the actual room in the house. For every inch in the diagram, the real room is 10 feet.

Use your ruler to find the dimensions of the diagram. Put the actual lengths on the slightly larger diagram.

What is the relationship between the diagram and the actual room? ________________________
________________________________________________________________________

Why is it useful for architects to make models? _________________________________
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
Station 3

At this station, you will find a model car and the scale factor that describes the relationship between the size of the model and the real car.

Draw a diagram of this car in the space below without the measurements.

Use the scale factor to set up appropriate proportions. Show your work below.

Write the measurements of the real car on your drawing.

Discuss with your group. What word describes the relationship between the model car and the real car—congruent or similar? Explain.
Station 4

At this station, you will find a ruler and a calculator. You will use these to look at the relationship between the areas of similar triangles.

Look at the triangles below.

What is the area of the smaller triangle? ___________________

What is the area of the larger triangle? ___________________

What is the ratio of area of the larger triangle to the smaller triangle? ___________________

Draw your own triangle. Measure the height and the base. Create a triangle with sides that are twice as long. Find the area of the two triangles.

Area of small triangle: __________
Area of large triangle: __________
Ratio of area of large triangle to area of small triangle: __________

Discuss with your group. What is true about the area of similar triangles when the sides are increased by a factor of two?

________________________________________________________________________

________________________________________________________________________

Why do you think this is true? ____________________________________________

________________________________________________________________________

________________________________________________________________________
Geometry

Set 3: Sketching, Modeling, and Describing 3-D Figures

Goal: To provide opportunities for students to develop concepts and skills related to sketching, modeling, and describing the cross-sections of three-dimensional figures

Common Core Standards

Geometry

Draw, construct, and describe geometrical figures and describe the relationships between them.

7.G.3. Describe the two-dimensional figures that result from slicing three-dimensional figures, as in plane sections of right rectangular prisms and right rectangular pyramids.

Student Activities Overview and Answer Key

Station 1

Students use clay and mold it into a cone. They then cut the cone in various directions and observe how the different cuts produce different cross-sections.

Answers: circle; parabola or part of an ellipse; an ellipse; the cross-sections are different depending on what way we cut the cone

Station 2

Students explore the cross-sections of a rectangular prism. They draw cross-sections from three different cuts. They then notice the similarities between the cuts.

Answers: rectangle; rectangle; rectangle; they are all rectangles

Station 3

Students have three cross-sections of a solid, and use this information to determine what solid the cross-sections are from. They then explain their strategy for successfully completing this task.

Answers: a pyramid; answers will vary
Station 4

Students use three marshmallows to investigate the cross-sections of a cylinder. They draw each cross-section, and then compare and contrast the results.

Answers: Answers will vary.

Materials List/Setup

<table>
<thead>
<tr>
<th>Station</th>
<th>Items</th>
</tr>
</thead>
<tbody>
<tr>
<td>Station 1</td>
<td>clay; plastic knives</td>
</tr>
<tr>
<td>Station 2</td>
<td>a rectangular prism</td>
</tr>
<tr>
<td>Station 3</td>
<td>none</td>
</tr>
<tr>
<td>Station 4</td>
<td>3 marshmallows; a plastic knife</td>
</tr>
</tbody>
</table>
Discussion Guide

To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions

1. What is an example of when you see the cross-section of a rectangular prism?
2. How would you get a point as a cross-section in a cone?
3. What are two figures that have the same shaped cross-sections (not necessarily the same size) if you cut them horizontally, vertically, and diagonally?
4. What are two figures that have different shaped cross-sections if you cut them horizontally, vertically, and diagonally?

Think, Pair, Share

Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses

1. many examples—at the deli when they cut cheese
2. make a slice at the very tip of the point of the cone
3. sphere, cube, rectangular prism
4. many examples—cylinder, pyramid, cone, etc.

Possible Misunderstandings/Mistakes

- Having trouble visualizing cross-sections
- Having trouble cutting the clay or marshmallows
- Confusing any of the three different cross-sections
Station 1

At this station, you will find clay and plastic knives.

Mold your clay into a cone. Make a horizontal cut. What shape do you get when you look down at the cut? Draw what you see.

Mold your clay back into a cone. Make a vertical cut. What shape do you get when you look down at the cut? Draw what you see.

Mold your clay into a cone for the third time. Make a diagonal cut. What shape do you get when you look down at the cut? Draw what you see.

How does the direction of the cross-section of a cone change what it looks like? Discuss with your group.
Station 2

At this station, you will find a rectangular prism which will help you visualize different cross-sections. Discuss and answer the question below.

If you made a horizontal cut, what would the cross-section look like? Draw it below.

If you made a vertical cut, what would the cross-section look like? Draw it below.

If you made a diagonal cut, what would the cross-section look like? Draw it below.

What do you notice about all three cross-sections? ________________________________________
_________________________________________________________________________________
_________________________________________________________________________________
Station 3

At this station, you will be looking at a set of cross-sections and using them to figure out what solid they are from.

Look at the cross-sections below. They are horizontal, vertical, and diagonal, in that order.

What solid is each cross-section from? Discuss with your group.

__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________

Explain your strategy for figuring that out. ____________________________________
__________________________________________________________________________
__________________________________________________________________________

A cone is similar to a pyramid, except with a circle base. Draw the cross-sections of a cone below.
Station 4

At this station, you will find three marshmallows and a plastic knife. You will use these to investigate the cross-sections of a cylinder.

Cut the first marshmallow horizontally. What does it look like? Draw the cross-section below.

Cut the second marshmallow vertically. What does it look like? Draw the cross-section below.

Cut the third marshmallow diagonally. What does it look like? Draw the cross-section below.

Discuss with your group. Describe the similarities and differences in the cross sections.
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
Statistics and Probability

Set 1: Collecting, Organizing, and Analyzing Data

Goal: To provide opportunities for students to develop concepts and skills related to data collection and analysis

Common Core Standards

Statistics and Probability

Investigate chance processes and develop, use, and evaluate probability models.

7.SP.5. Understand that the probability of a chance event is a number between 0 and 1 that expresses the likelihood of the event occurring. Larger numbers indicate greater likelihood. A probability near 0 indicates an unlikely event, a probability around 1/2 indicates an event that is neither unlikely nor likely, and a probability near 1 indicates a likely event.

7.SP.6. Approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency, and predict the approximate relative frequency given the probability.

7.SP.7. Develop a probability model and use it to find probabilities of events. Compare probabilities from a model to observed frequencies; if the agreement is not good, explain possible sources of the discrepancy.

b. Develop a probability model (which may not be uniform) by observing frequencies in data generated from a chance process.

7.SP.8. Find probabilities of compound events using organized lists, tables, tree diagrams, and simulation.

Student Activities Overview and Answer Key

Station 1

Students will be generating their own data and turning it into a scatter plot. They will examine and answer questions pertaining to this scatter plot.

Answers: answers may vary; answers may vary

Station 2

Students will formulate different questions that they would be able to go out and collect data for, remembering that it is important to collect enough data to draw valid conclusions. They then choose one question to look at more closely. Students reflect on how they would work towards answering that question, and why it is important to collect a lot of data.
Answers: answers may vary; answers may vary; answers may vary; answers may vary; If we do not collect enough data, we will not be able to see true trends in the data.

Station 3
Students try to answer the question of which side of a number cube comes up most. They conduct an experiment to help answer this question, and then develop other questions that could be answered by their data.

Answers: answers may vary; answers may vary; answers may vary, for example, Which number comes up least? Do all numbers come up about the same number of times?

Station 4
Students roll a number cube and find the mean at different intervals. They then compare the means and determine which is closest to the expected value. This helps point out why it is important to have a large sample size (30 or more).

Answers: answers will vary; answers will vary; answers will vary; the mean of 30 rolls should be closest to the expected value of a roll; the mean of 30 rolls should be closest to 3.5 because there was an opportunity to account for flukes of many high or low rolls.

Materials List/Setup
Station 1 two number cubes (1–6)
Station 2 none
Station 3 number cube (1–6)
Station 4 number cube (1–6)
Discussion Guide

To support students in reflecting on the activities and to gather some formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions

1. What conclusions can you draw from a scatter plot if all the points are in a line? What if the points are randomly distributed?
2. Why is it important to collect a lot of data when conducting research?
3. What is an example of a real-life situation where we might want to conduct a survey to answer a question?
4. How does conducting an experiment help us answer questions?

Think, Pair, Share

Have students jot down their own responses to questions, then discuss with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses

1. If the points are in a line, there is a correlation between the two variables. If the points are randomly distributed, one variable does not affect the other.
2. because if you don’t collect enough data, you won’t notice the trends
3. anything where we care what a specific population does, wants, etc., such as how much money most people spend at lunch
4. It lets us see how frequently we get different outcomes and what those outcomes are.

Possible Misunderstandings/Mistakes

- Not asking questions that can be answered by collecting data
- Developing questions that are too broad (e.g., What is your name?)
- Not properly labeling the graph
- Confusing the axes
Station 1

At this station, you will find two number cubes. You will be using these number cubes to generate data which you will then graph.

You will roll the number cubes one at a time. Record the number that comes up on the first number cube. Roll the second number cube, and record the sum of the two number cubes. Do this 30 times and record the data in the table below.

<table>
<thead>
<tr>
<th>First number cube</th>
<th>Second number cube</th>
<th>Sum of number cubes</th>
<th>First number cube</th>
<th>Second number cube</th>
<th>Sum of number cubes</th>
</tr>
</thead>
<tbody>
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</table>

Using this data, create a scatter plot on a separate sheet of paper. Be sure to title the scatter plot and use appropriate labels.

What is the range of the sums? __________________

What do you notice about your scatter plot? Is there a general trend?
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
Station 2

At this station, you will come up with different questions you could answer by collecting data.

Work with your group to come up with five questions you could answer by going out and collecting data. You need to be able to collect at least 30 pieces of data in order to answer any of these questions. (For example, what is the average number of siblings students in our class have?)

__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________
__________________________________________________________________________

Choose one of those questions to focus on.

How would you gather data to answer your question? Make sure to gather at least 30 pieces of data.

__________________________________________________________________________
__________________________________________________________________________

What materials would you need to gather the data? (e.g., number cubes)

__________________________________________________________________________
__________________________________________________________________________

How would you present your data? (e.g., bar graph, table)

__________________________________________________________________________
__________________________________________________________________________

Why is it important that you collect at least 30 pieces of data? Why are 5 pieces not enough?

__________________________________________________________________________
__________________________________________________________________________
Station 3

At this station, you will try to determine which side of a number cube comes up most often.

Each member of your group should roll a number cube 25 times, keeping track of how many times each number comes up.

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<th>Tally</th>
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</table>

Combine your data in the table below.

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<th>Total</th>
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</tbody>
</table>

Based on this data, which number do you think has the best chance of coming up? ________

Some people say that they roll a 1 more often than a 6. Does your data support that statement? Explain.

________________________________________________________________________

________________________________________________________________________

________________________________________________________________________

What are two questions you could answer with this data?

________________________________________________________________________

________________________________________________________________________

________________________________________________________________________
Station 4

At this station, you will find a number cube.

Roll the number cube 5 times and record your results in the table below.

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<th>Tally</th>
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</table>

What is the value of the mean roll? ________

Now roll the number cube 10 times. Record your results below.

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<th></th>
<th>Tally</th>
<th>Final number</th>
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<tbody>
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<td>1</td>
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<td>6</td>
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</table>

What is the value of the mean roll? ________

continued
Finally, roll the number cube 30 times. Record your results below.

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<th>Final number</th>
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</table>

As a group, review your data and answer the following questions.

What is the value of the mean roll? ________

How do the three means compare? What do you notice? ______________________________________
____________________________________________________________________________________
____________________________________________________________________________________

The mean value of the number cube is 3.5. Which mean is closest to that value? Why?
____________________________________________________________________________________
____________________________________________________________________________________
____________________________________________________________________________________
Statistics and Probability

Set 2: Theoretical Probability

Goal: To provide opportunities for students to develop concepts and skills related to theoretical probability

Common Core Standards

Statistics and Probability

Investigate chance processes and develop, use, and evaluate probability models.

7.SP.5. Understand that the probability of a chance event is a number between 0 and 1 that expresses the likelihood of the event occurring. Larger numbers indicate greater likelihood. A probability near 0 indicates an unlikely event, a probability around 1/2 indicates an event that is neither unlikely nor likely, and a probability near 1 indicates a likely event.

7.SP.6. Approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency, and predict the approximate relative frequency given the probability.

Student Activities Overview and Answer Key

Station 1
Students will look at two pairs of number cubes. They will compare the probability of rolling particular sums. In the end, they will draw conclusions about the two pairs of number cubes.

Answers: 1/6; 5/36; 1/6; 5/36; The probability of rolling each sum is the same for both pairs of number cubes.

Station 2
Students will consider two different spinners. They determine the theoretical probability of spinning various colors. They then work toward determining the probability of having one land on one color and the other land on another color, and discuss their strategy for this task.

Answers: 1/4; 1/4; 1/2; 1/2; 1/8; using a tree diagram, writing out all the possibilities, multiplying 4 × 2

Station 3
Students will use a tree diagram to show the possible combinations when rolling two number cubes. They will use their diagram to answer questions about the likeliness of rolling different sums.

Answers: 11; no, because some sums repeat themselves; rolling a 7: the sum is 7 six times.
Station 4

Students find the theoretical probability for drawing cubes out of a bag. They then consider how the probabilities would be affected if everything in the bag was doubled, and draw conclusions.

**Answers:** \(\frac{1}{5}; \frac{1}{5}; \frac{2}{5};\) because there are twice as many yellow cubes as any other color; \(\frac{2}{10}\) or \(\frac{1}{5}\); \(\frac{4}{10}\) or \(\frac{2}{5}\); the probabilities do not change

**Materials List/Setup**

**Station 1**

two number cubes with the following sides:
(4, 2, 2, 1, 3, 3) and (6, 1, 3, 5, 4, 8)

**Station 2**
two spinners; the first one should be divided evenly into red, green, blue, and yellow sections; the other should be evenly divided into black and white sections

**Station 3**

ruler

*optional:* two number cubes (1–6)

**Station 4**

bag containing one each of red, blue, and green cubes, and two yellow cubes
Instruction

Discussion Guide

To support students in reflecting on the activities, and to gather formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions

1. In what real-life situation might it be good to know the theoretical probability of an event happening?

2. You have 10 blocks in a bag—5 red, 2 yellow, 1 blue, and 2 green—and have figured out the probability of drawing a red block. Now you triple the number of blocks in the bag (15 red, 6 yellow, 3 blue, and 6 green). How does this affect the theoretical probability?

3. Make a general statement about what happens to the probability of an event happening (pulling out a red block, for example) if we multiply each choice by the same number.

4. How can tree diagrams help you determine theoretical probabilities?

Think, Pair, Share

Have students jot down their own responses to questions, discuss their responses with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses

1. when buying a lottery ticket—you might decide not to since the odds are against you

2. It does not affect it.

3. The probability does not change.

4. They show you all the possible outcomes.

Possible Misunderstandings/Mistakes

- Not understanding that the ratio \(\frac{2}{5}\) is equivalent to \(\frac{4}{10}\)
- Miscounting the number of answers that satisfy the probability you are looking for
- Flipping the ratios (e.g., \(\frac{5}{2}\) instead of \(\frac{2}{5}\))
Station 1

At this station, you will find a very special pair of number cubes.

The table below shows the values on each number cube. Fill in the possible sums.

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</tbody>
</table>

What is the theoretical probability of rolling a 6? Write your solution as a ratio. ______________

What is the theoretical probability of rolling an 8? Write your solution as a ratio. ______________

Below is a table of all the sums possible when rolling two regular number cubes (sides 1–6).

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<td>11</td>
<td>12</td>
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</tbody>
</table>

What is the theoretical probability of rolling a 6? Write your solution as a ratio. ______________

What is the theoretical probability of rolling an 8? Write your solution as a ratio. ______________

Look at both tables closely. What do you notice? ______________________________________
__________________________________________________________________________
__________________________________________________________________________
Station 2
At this station, you will find two spinners. One spinner is evenly divided into four colors—red, green, blue, and yellow.

Work with your group to determine the following probabilities. Write them as a ratio.

\[ P(\text{yellow}) = \] ________________

\[ P(\text{red}) = \] ________________

The second spinner is evenly divided into two colors—black and white.

Work with your group to determine the following probabilities. Write them as a ratio.

\[ P(\text{black}) = \] ________________

\[ P(\text{white}) = \] ________________

What is the probability of spinning yellow and white? Use a tree diagram to draw out the different options, if necessary.

What strategy did you use to determine the probability of spinning yellow and white?

__________________________________________________________________________
__________________________________________________________________________
Station 3

At this station, you will use a tree diagram to help you figure out the theoretical probability of different totals you could get when rolling two number cubes.

Draw a tree diagram to show all the possible combinations of rolls if your number cubes are both numbered 1–6.

Write the probability of getting each total as a ratio on your tree diagram.

How many different possible totals can you get by rolling two number cubes? ______________

Are all the totals equally likely? How do you know? ____________________________________
__________________________________________________________________________
__________________________________________________________________________

Which outcome is most likely? How do you know? ____________________________________
__________________________________________________________________________
Station 4

At this station, you will be working on determining theoretical probability. You will see a bag with five cubes in it—one green, one blue, one red, and two yellow.

You should imagine what would happen if you pulled out one cube. Find the following theoretical probabilities. Be sure to write the probabilities as ratios.

\[ P(\text{green}) = \frac{\text{number of green cubes}}{\text{total number of cubes}} = \frac{1}{5} \]

\[ P(\text{blue}) = \frac{\text{number of blue cubes}}{\text{total number of cubes}} = \frac{1}{5} \]

\[ P(\text{yellow}) = \frac{\text{number of yellow cubes}}{\text{total number of cubes}} = \frac{2}{5} \]

Why is the probability of pulling out a yellow different from the probability of drawing another color?
________________________________________________________________________
________________________________________________________________________

What would the probability of drawing a red be if we doubled the blocks that were in the bag (2 green, 2 blue, 2 red, and 2 yellow)? ______________

What would the probability be of drawing a yellow in this same situation? ______________

What do you notice about the probabilities if we double everything in the bag?
________________________________________________________________________
________________________________________________________________________
________________________________________________________________________
Statistics and Probability
Set 3: Experimental Probability

Goal: To provide opportunities for students to develop concepts and skills related to understanding experimental probability and theoretical probability

Common Core Standards
Statistics and Probability
Investigate chance processes and develop, use, and evaluate probability models.

7.SP.6. Approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency, and predict the approximate relative frequency given the probability.

7.SP.7. Develop a probability model and use it to find probabilities of events. Compare probabilities from a model to observed frequencies; if the agreement is not good, explain possible sources of the discrepancy.

a. Develop a uniform probability model by assigning equal probability to all outcomes, and use the model to determine probabilities of events.

b. Develop a probability model (which may not be uniform) by observing frequencies in data generated from a chance process.

Student Activities Overview and Answer Key
Station 1
Students will predict the number of times they will pull a red, green, and blue block from a bag. They will use theoretical probability to make this prediction. Students will then draw a cube from the bag and replace it 36 times in intervals of 12. They will compare their experimental results along the way with the theoretical results, and draw conclusions.

Answers: First table—4, 8, 12; second set of tables—answers vary depending on what blocks are pulled out; answers vary depending on what blocks are pulled out; answers may vary, but most likely students will be closer to their prediction for 36 turns than for 12 turns; Yes, the more turns we have, the closer the experimental probability is to the theoretical probability.

Station 2
Students will work with a list of randomly generated numbers. They predict what the mean should be based on the experimental probability of getting each number. They then compare their prediction with the actual average in a series of intervals. They will compare their experimental results with the theoretical result, and draw conclusions.
Statistics and Probability
Set 3: Experimental Probability

Answers: 5; table—answers will vary; The mean should approach the prediction as the amount of numbers increases; The experimental mean should be 5.

Station 3
Students will find the theoretical probability for rolling a 5 on a number cube. They will then each roll the number cube 20 times and compare the experimental probability to the theoretical probability. They will repeat this comparison after combining group data. Students then draw conclusions about sample size and experimental probability.

Answers: $\frac{1}{6}$; answers will vary; answers will vary; answers will vary—probably the second number because there was a larger sample size, and as sample size increases, experimental probability approached theoretical probability

Station 4
Students individually flip a coin 50 times to generate data. They then combine their data and look at the percentage of heads and tails that come up. Students discuss what the breakdown would look like if they flipped the coin 100,000 times.

Answers: Answers will vary; answers will vary; about 50% each because the experimental probability approaches the theoretical probability when sample sizes are very large

Materials List/Setup
Station 1 three blocks (red, green, and blue); a bag
Station 2 list of 100 randomly generated numbers (1–9)
Station 3 number cubes for each group member (1–6)
Station 4 coin for each group member
Discussion Guide

To support students in reflecting on the activities, and to gather formative information about student learning, use the following prompts to facilitate a class discussion to “debrief” the station activities.

Prompts/Questions

1. Why do we need a large sample size for the experimental probability to approach the theoretical probability?
2. Why do small samples differ from the theoretical probability?
3. Why is it important that we use random numbers or randomly pull a block out of the bag?
4. If you flipped a coin 1,000,000 times, how many times do you think heads would come up?

Think, Pair, Share

Have students jot down their own responses to questions, discuss their responses with a partner (who was not in their station group), and then discuss as a whole class.

Suggested Appropriate Responses

1. Large sample sizes account for any unusual outcomes that small sample sizes do not (e.g., rolling five 6s in a row).
2. Small samples can be affected by oddities in data.
3. Theoretical probability is not biased, so we should try to eliminate bias from experimental probability.
4. about 500,000 times

Possible Misunderstandings/Mistakes

- Difficulty dealing with a large amount of data
- Expecting small samples to look like the theoretical probability
- Thinking that when they have 30 or more pieces of data, the experimental probability will look exactly like the theoretical probability
At this station, you will find three blocks in a bag—one red, one green, and one blue. Imagine that you pull out a block, record what color it is, and put it back in.

Work with your group to determine how many times you would expect to pull out the green block if you went through this routine 12 times, 24 times, and 36 times. This should be the theoretical probability. Record your predictions in the table below.

<table>
<thead>
<tr>
<th>Number of times you choose a block</th>
<th>Predicted number of green blocks you will choose</th>
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</thead>
<tbody>
<tr>
<td>12</td>
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<tr>
<td>24</td>
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<td>36</td>
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</tbody>
</table>

Now we are going to test our predictions. Place the three blocks in the bag. Without looking, take one block out. Record the color of the block you pulled out in the table below. Also, total the number of green blocks you pulled out after every 12 turns. Then answer the questions on the next page.

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<th>Turn</th>
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<th>6</th>
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<th>Turn</th>
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<th>31</th>
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continued
How close were your original predictions? ________________________________________________

Were you closer with your guess about how many green blocks would be pulled after 12 turns or after 36 turns?

_______________________________________________________________________________

Do you think you would be even closer if you had to estimate how many green blocks you would pull out after 300 turns? Why or why not?

_______________________________________________________________________________

_______________________________________________________________________________

_______________________________________________________________________________
Station 2

At this station, you have a list of 100 randomly generated numbers. Each number, 1–9, has an equally likely chance of coming up.

If the experimental probability of a number coming up is \( \frac{1}{9} \) for every number, what do you think the mean of your list of numbers will be?

___________________

Use the list of randomly generated numbers to fill in the table below. Under “Sum,” write the total sum of the first 25, 50, 75, and 100 numbers. For “Mean,” determine the mean of the set of data up to that point.

<table>
<thead>
<tr>
<th>Amount of numbers</th>
<th>Sum</th>
<th>Mean</th>
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<tbody>
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<td>100</td>
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</table>

What do you notice about your mean prediction as the amount of numbers you look at increases?

__________________________________________________________________________

__________________________________________________________________________

What do you think would happen if you found the mean of 10,000 randomly generated numbers (1–9)? Explain.

__________________________________________________________________________

__________________________________________________________________________
Station 3

At this station, you will find enough number cubes for each group member. Each group member should take one number cube. Work as a group to answer the following question.

What is the probability of rolling a 5? ___________________

Now each group member will roll a number cube 20 times on his or her own, and record the rolls in the table below.

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<thead>
<tr>
<th>Tally</th>
<th>Total number</th>
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<tbody>
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<td>1</td>
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</table>

What was the experimental probability of rolling a 5? ___________________

Combine data with your group.

<table>
<thead>
<tr>
<th>Total number</th>
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<tbody>
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</table>

What is the experimental probability of rolling a 5? ___________________

Which experimental probability was closer to the theoretical probability? Why?

__________________________________________________________________________
__________________________________________________________________________
Station 4

You will find a coin for every group member at this station.

Each group member should flip the coin 50 times, and record his or her data in the table below.

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<thead>
<tr>
<th></th>
<th>Tally</th>
<th>Total number</th>
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</thead>
<tbody>
<tr>
<td>Heads</td>
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<td></td>
</tr>
<tr>
<td>Tails</td>
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</tbody>
</table>

Now combine data with your group members.

<table>
<thead>
<tr>
<th></th>
<th>Total number</th>
</tr>
</thead>
<tbody>
<tr>
<td>Heads</td>
<td></td>
</tr>
<tr>
<td>Tails</td>
<td></td>
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</tbody>
</table>

What percentage of the flips was heads? ____________________

What percentage of the flips was tails? ____________________

What do you think the percentages would be if you flipped the coin 100,000 times? Why?
______________________________________________________________________
______________________________________________________________________